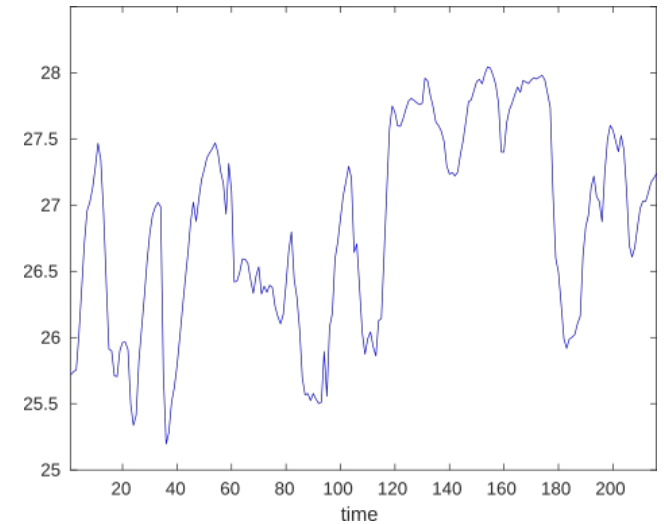
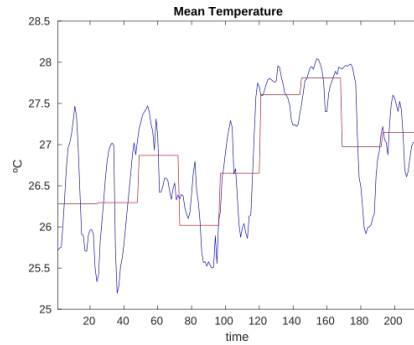
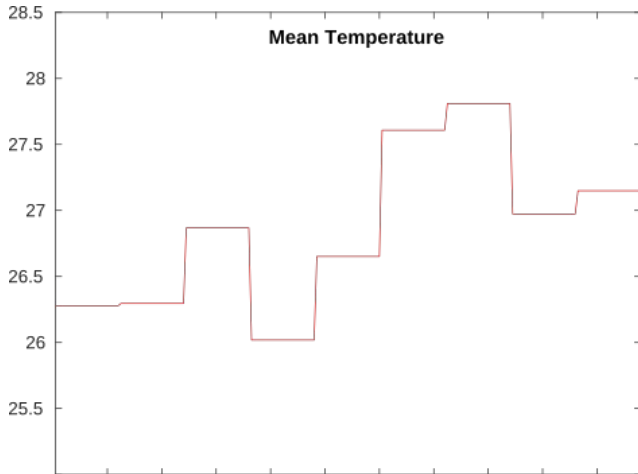




<http://www.meteo.unican.es>

# From daily to sub-daily climate projections: Increasing the temporal resolution by means of statistical downscaling



$$Y = f(X; \theta)$$



**Sixto Herrera**  
sixto.herrera@unican.es

**Meteorology Group**  
Univ. de Cantabria – CSIC  
MACC/IFCA



## ❖ ***Motivation***

***Impact models' requirements ↔ Statistical Downscaling***

## ❖ ***Statistical downscaling***

***Transfer Functions***

***Weather Typing - Analogues***

***Weather Generators***

***Analog-based methods***

## ❖ ***Conclusions***

# Motivation: Impact Models

## climate projections

RCP scenarios from CMIP  
& CORDEX archives

## Socio-economic input

SSP scenarios

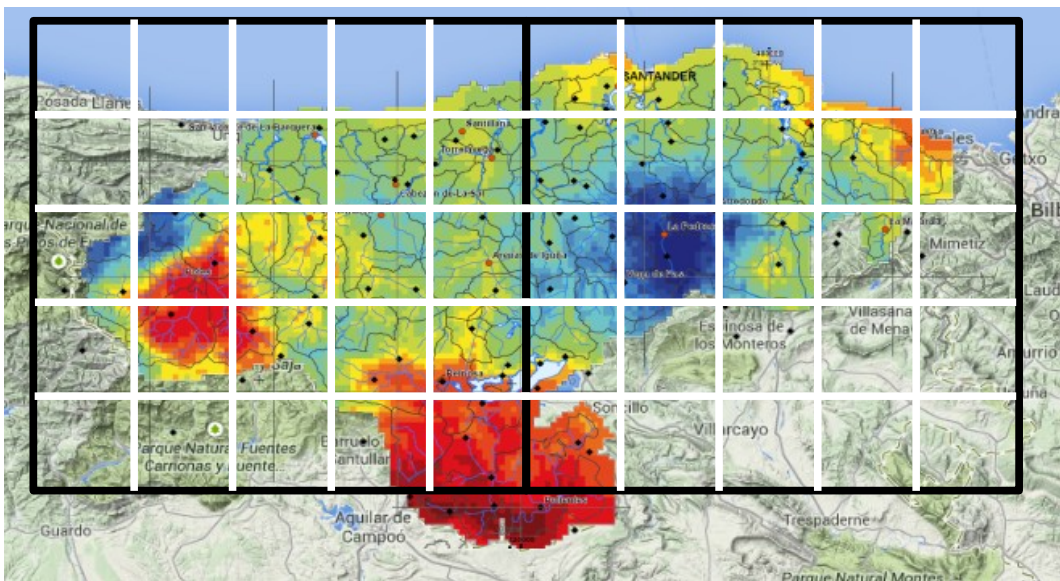
## Impact models global & regional

agriculture  
biomes  
coastal infrastructure  
fisheries  
agro-economics

water  
Forests  
health  
energy  
permafrost

- Synthesis of impacts at different levels of global warming
- Quantification of uncertainties
- Model improvement
- Cross-sectoral interactions
- Cross-scale intercomparison
- Focus topics (e.g. extreme events, adaptation)

<https://www.isimip.org/about/>



Impact Models' needs:

- local or very high spatial resolution (~ 1km).

**Spatial statistical downscaling**  
**Challenges and prospects on the road to**  
**1km ISIMIP3b daily climate data**

Black cells ~ 100 km (GCMs, CMIP)

White cells ~ 10 km (RCMs, CORDEX)



# Motivation: Impact Models

## climate projections

RCP scenarios from CMIP & CORDEX archives

## Socio-economic input

SSP scenarios

## Impact models global & regional

agriculture  
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## Floods Urban drainage



## Impact Models' needs:

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- Some extreme events have temporal resolutions lower than daily.

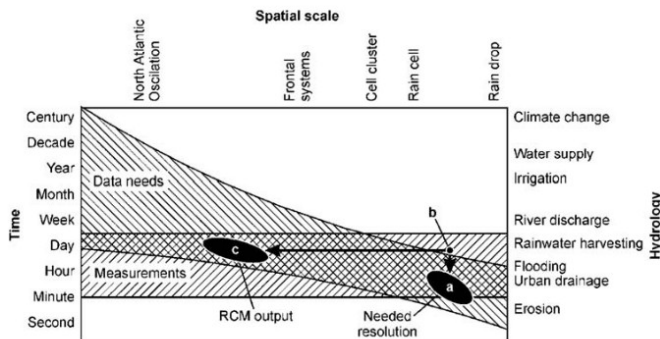
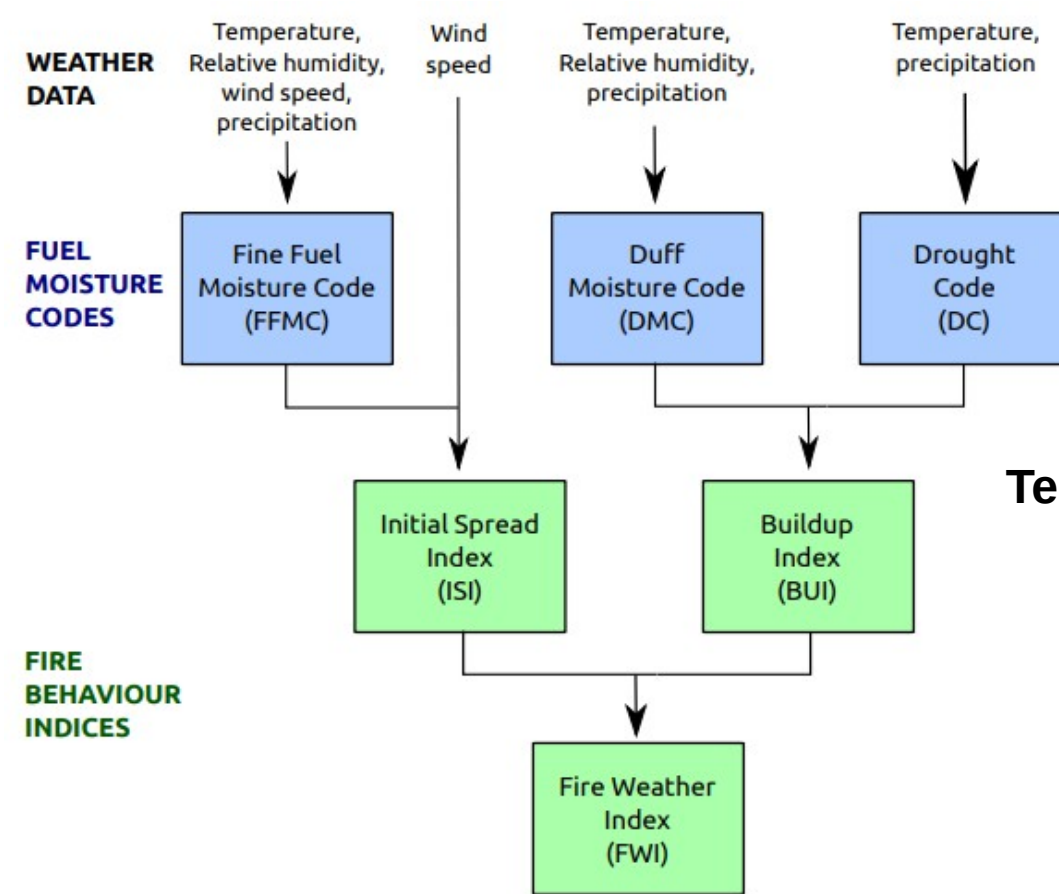


Figure 7.2 Statistical downscaling of RCM outputs down to the scale required for urban hydrological impact studies requires both temporal downscaling (a-b) and spatial downscaling (b-c) (adapted from Ambjerg-Nielsen, 2008).

## Santander Meteorology Group

*A multidisciplinary approach for weather & climate*

# Motivation: Impact Models



Fire

Temperature, humidity and wind speed at noon

Impact Models' needs:

- local or very high spatial resolution (~ 1km).
- Some extreme events have temporal resolutions lower than daily.
- Some communities need of subdaily data.

Figure 3.6: Block diagram of the CFFWIS (Adapted from van Wagner, 1987).

# Motivation: Impact Models



You are at the [ESGF-DATA.DKRZ.DE](#) node

Home

Technical Support

**Project**

CORDEX (165003)

**Product**

**Domain**

**Institute**

**Driving Model**

**Experiment**

**Experiment Family**

**Ensemble**

**RCM Model**

**Downscaling Realisation**

**Time Frequency**

1hr (847)

3hr (8378)

6hr (10375)

day (50004)

fx (2628)

mon (52854)

sem (39917)

**Variable**

**Variable Long Name**

**CF Standard Name**

**Datanode**

Enter Text:

Display  results per page [\[ More Search Options \]](#)

Search Constraints:  CORDEX  Show All Replicas  Show All Versions  Search Local Node Only (Including All Replicas)

Total Number of Results: 165003

-1- 2 3 4 5 6 Next >>

Please login to add search results to your Data Cart

Expert Users: you may display the search URL and return results as XML or return results as JSON

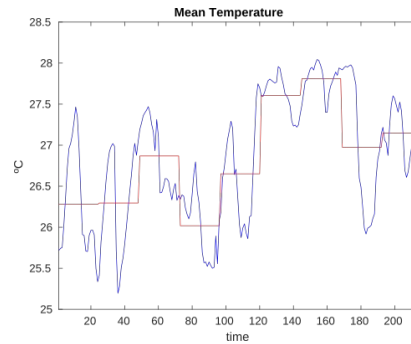
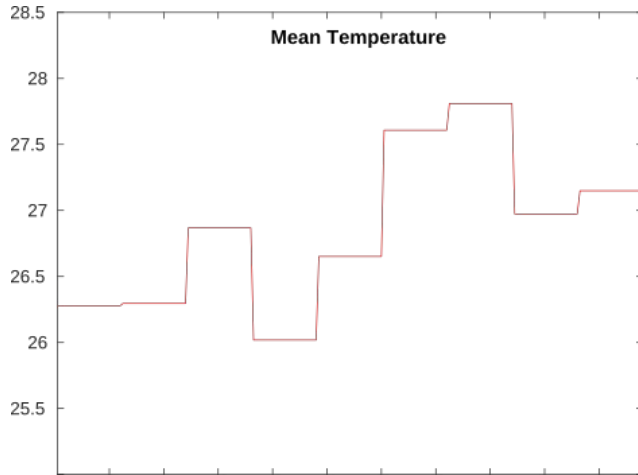
- cordex.output.AFR-44.DMI.ECMWF-ERAINT.evaluation.r1i1p1.HIRHAM5.v2.day.uas**  
Data Node: cordexesg.dmi.dk  
Version: 20140804  
Total Number of Files (for all variables): 5  
Full Dataset Services: [\[ Show Metadata \]](#) [\[ List Files \]](#) [\[ THREDDS Catalog \]](#) [\[ WGET Script \]](#)
- cordex.output.AFR-44.DMI.ECMWF-ERAINT.evaluation.r1i1p1.HIRHAM5.v2.day.uas**  
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## CORDEX: requested variables

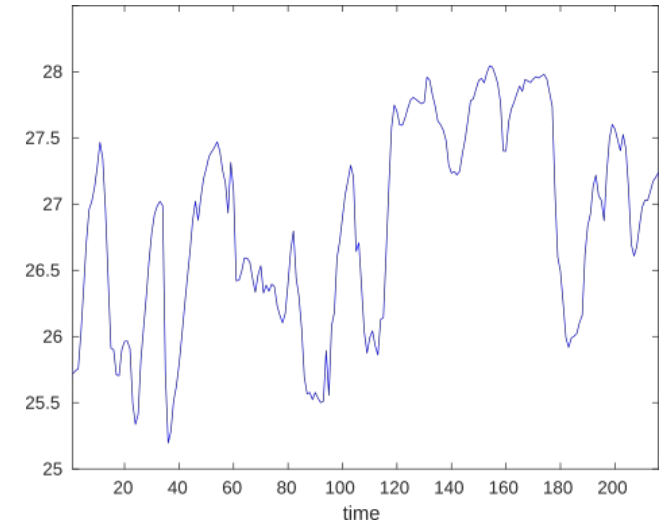
output variable name	units	Tier 2		Tier 1		Core			
		frq [1/day]	ag	frq [1/day]	ag	frq [1/mon]	ag	frq [1/sem]	ag
tas	K	8	i	1	8	1	m*8	1	s*8
tasmax	K			1		1	m	1	s
tasmin	K			1		1	m	1	s
pr	kg m-2 s-1	8	a	1		1		1	
ps	Pa	8	i	1	8				
psl	Pa	8	i	1	8	1	m*8	1	s*8
huss	1	8	i	1	8	1	m*8	1	s*8
hurs	%	8	i	1	8	1	m*8	1	s*8
sfcWind	m s-1	8	i	1	8	1	m*8	1	s*8
sfcWindmax	m s-1			1		1	m	1	s



# Motivation: Downscaling



$$Y = f(X; \theta)$$

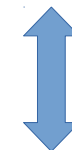


## CORDEX: requested variables

output variable name	units	Tier 2		Tier 1		Core			
		frq [1/day]	ag	frq [1/day]	ag	frq [1/mon]	ag	frq [1/sem]	ag
tas	K	8	i	1	8	1	m*8	1	s*8
tasmax	K			1		1	m	1	s
tasmin	K			1		1	m	1	s
pr	kg m <sup>-2</sup> s <sup>-1</sup>	8	a	1		1		1	
ps	Pa	8	i	1	8				
psl	Pa	8	i	1	8	1	m*8	1	s*8
huss	1	8	i	1	8	1	m*8	1	s*8
hurs	%	8	i	1	8	1	m*8	1	s*8
sfcWind	m s <sup>-1</sup>	8	i	1	8	1	m*8	1	s*8
sfcWindmax	m s <sup>-1</sup>			1		1	m	1	s

Impact Models' needs:

- local or very high spatial resolution (~ 1km).
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- Some communities need of subdaily data.



**Temporal statistical downscaling:  
Obtain sub-daily data from daily data**

# Statistical Downscaling

## Statistical Downscaling

### Transfer Functions

### Weather Generators

### Analogues Weather Typing

Links the local observed climate (predictand  $Y$ ) with the global simulations given by the GCMs (predictors  $X$ ), through some function  $f$  and/or parameters  $\theta$

Stochastic models able to generate artificial time series with similar statistical properties than the observed time series.

Similar atmospheric patterns lead to similar meteorological conditions (Lorenz, 1969). Based on the K-nearest neighbor algorithm.



## Transfer Functions

Links the local observed climate (**predictand Y**) with the global simulations given by the GCMs (**predictors X**), through some **function f** and/or **parameters  $\theta$**

A first approach is the so-called **delta method**, which assumes that the climate change signal at daily scale can be applied at hourly scale so it is “*added*” to the observations:

$$Y_{fut}^h = Obs^h + (Y_{fut}^{day} - Y_{ref}^{day})$$

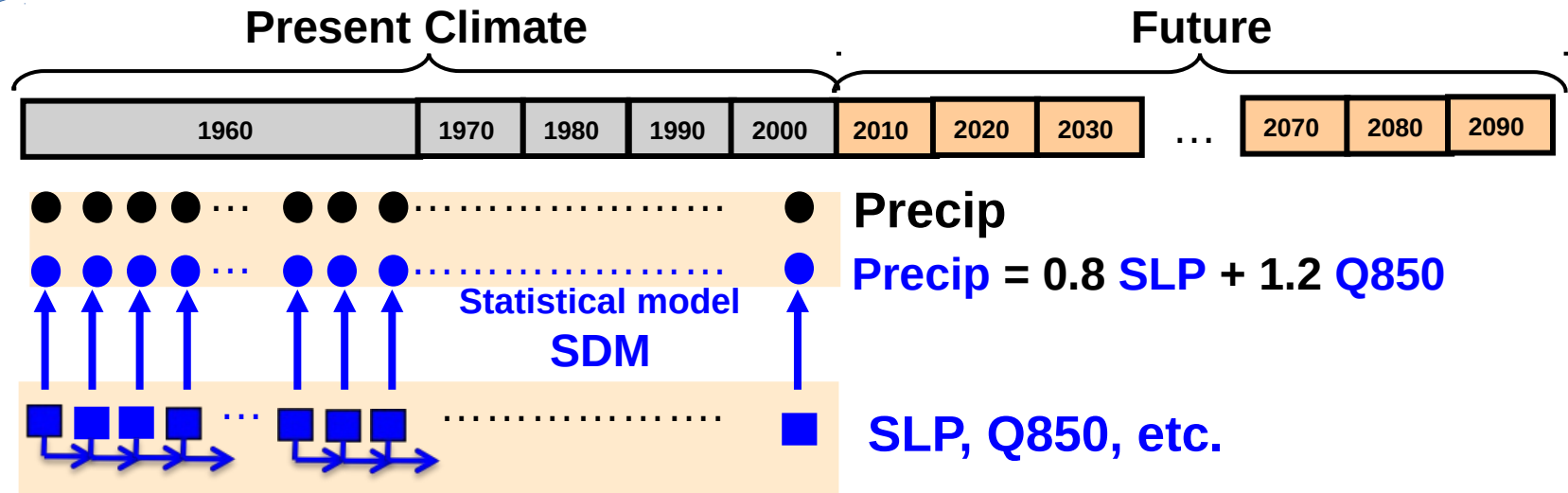
Several variations of this method have been proposed considering other moments of the statistical distribution (variance, quantiles, etc. See Willems and Vrac).

**The main shortcoming is that the daily cycle can not be modified, the observed is preserved for the projections.**

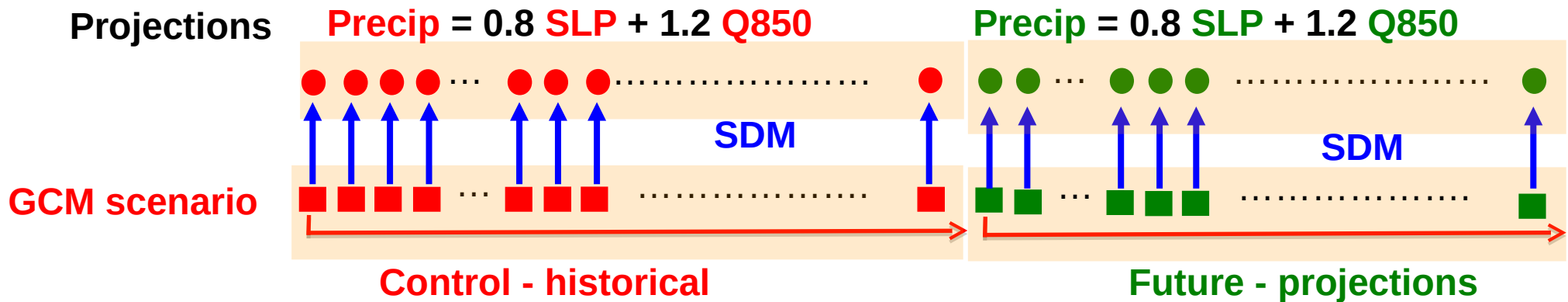
# Statistical Downscaling

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Links the local observed climate (**predictand Y**) with the global simulations given by the GCMs (**predictors X**), through some **function f** and/or **parameters  $\theta$**



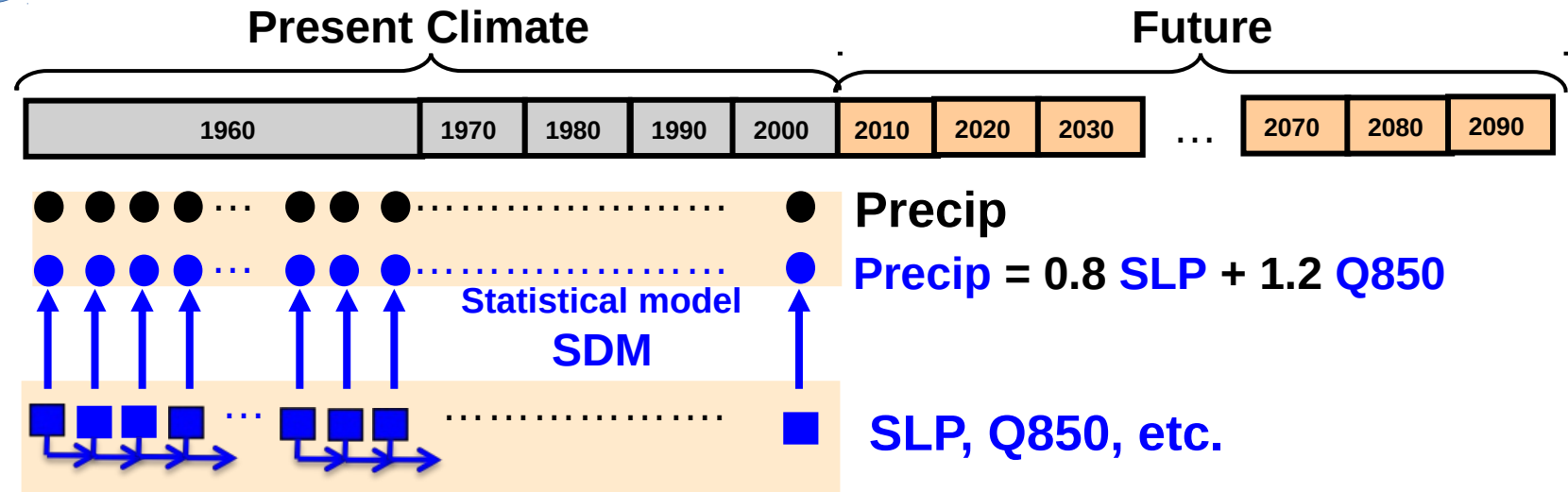
- Assumptions:** Reanalysis choice, choosing consistent predictors (e.g. sea level pressure and specific humidity) and stationarity/robustness.



# Statistical Downscaling

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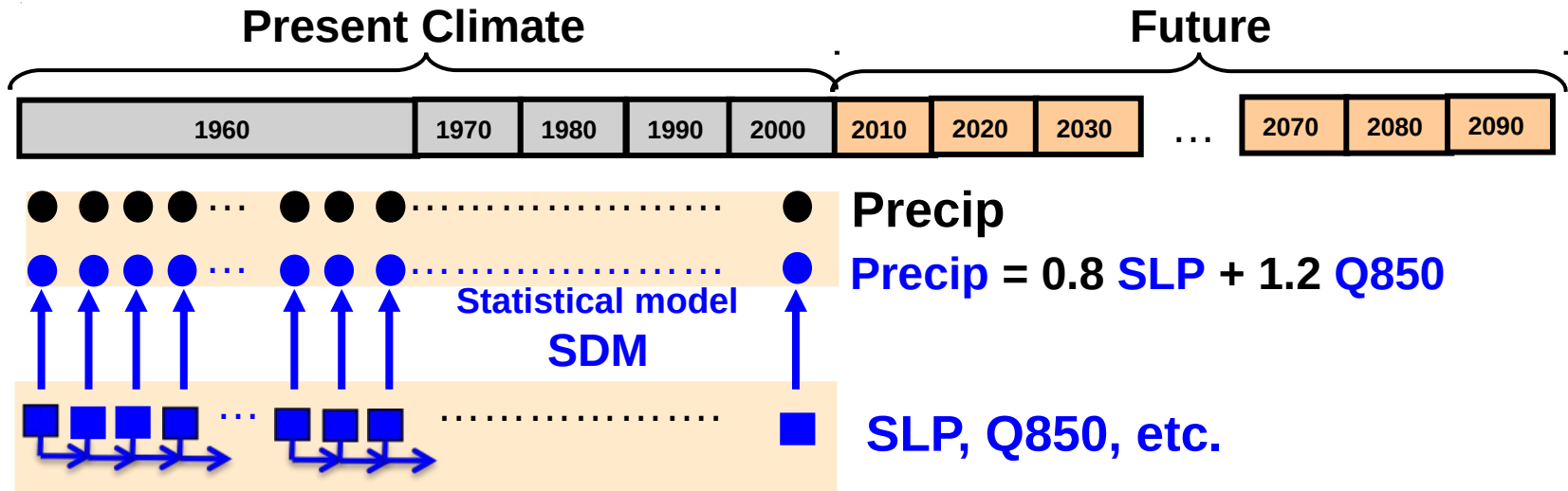
- **Assumptions:** Reanalysis choice, choosing consistent predictors (e.g. sea level pressure and specific humidity) and stationarity/robustness.
- **Assumptions:** There must be temporal consistency between observations, reanalysis and projections.



# Statistical Downscaling

Transfer Functions

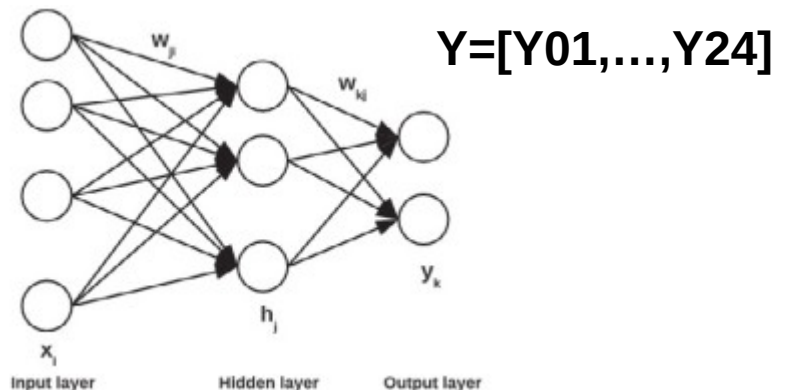
Links the local observed climate (**predictand Y**) with the global simulations given by the GCMs (**predictors X**), through some **function  $f$**  and/or **parameters  $\theta$**



- Adaptation:** Consider a model for each time step based on the same predictors to maintain some coherence between the predicted values.

Precip<sub>01h</sub> = a<sub>01</sub> SLP + b<sub>01</sub> Q850  
.....

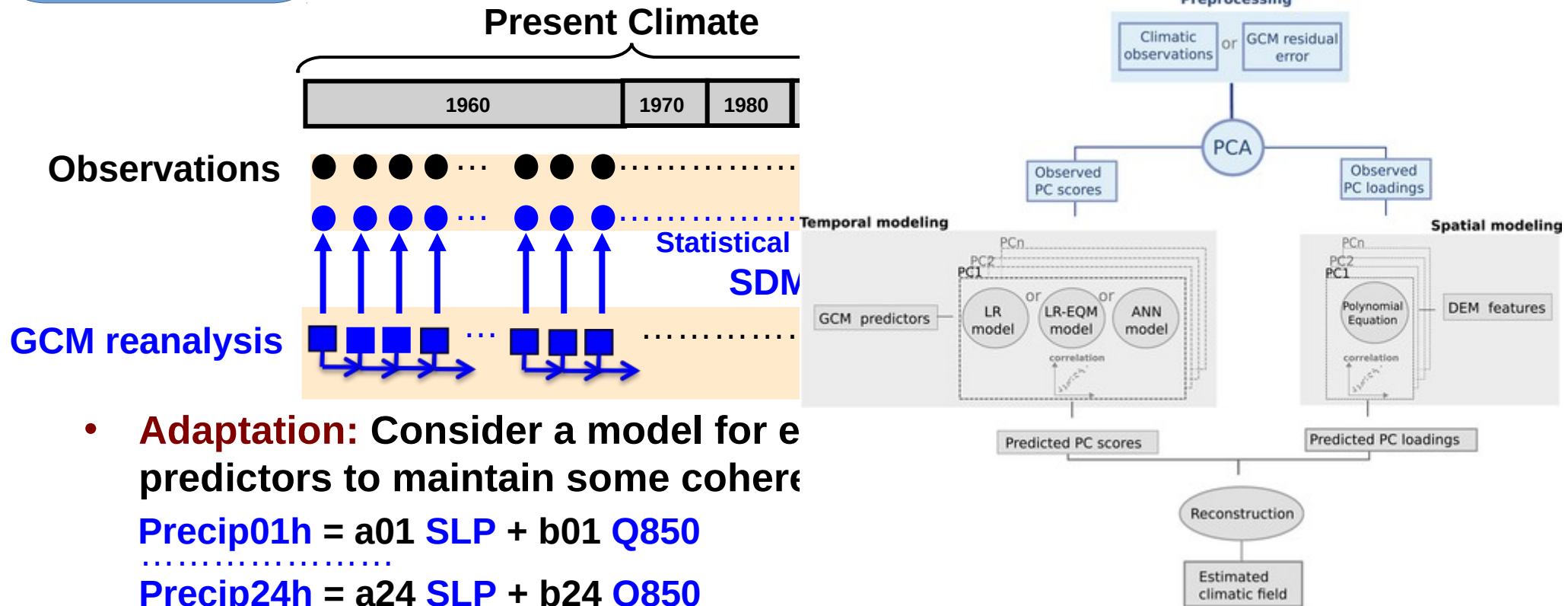
Precip<sub>24h</sub> = a<sub>24</sub> SLP + b<sub>24</sub> Q850



# Statistical Downscaling

## Transfer Functions

Links the local observed climate (**predictand Y**) with the global simulations given by the GCMs (**predictors X**), through some **function f** and/or **parameters  $\theta$**



- **Adaptation:** Consider a model for each predictor to maintain some coherence  

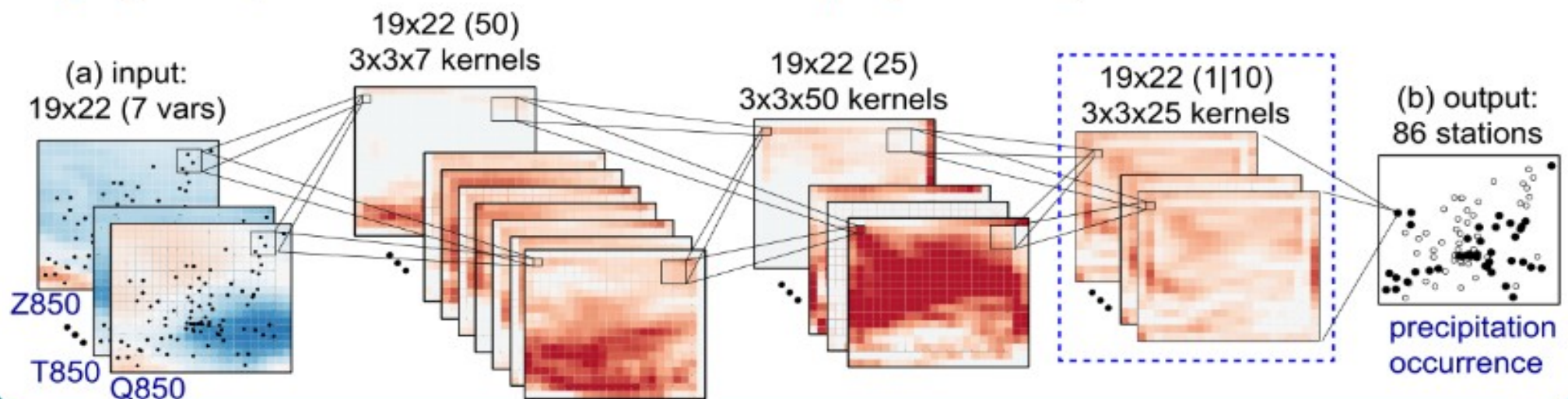
$$\text{Precip01h} = a_{01} \text{ SLP} + b_{01} \text{ Q850}$$

$$\text{Precip24h} = a_{24} \text{ SLP} + b_{24} \text{ Q850}$$
- **Adaptation:** Relate daily and sub-daily predictors (e.g. Martin et al. 2021).

# Pros and Cons

## Transfer Functions

- Transitions between the last hour of the previous day and the first one of the target day could not be preserved.
- Physical and spatial coherence between variables and location could not be preserved.
- These methods are commonly strongly dependent on the region, variable, season, etc. → New approaches, as Convolution Neural Networks, can partially solve this problem.

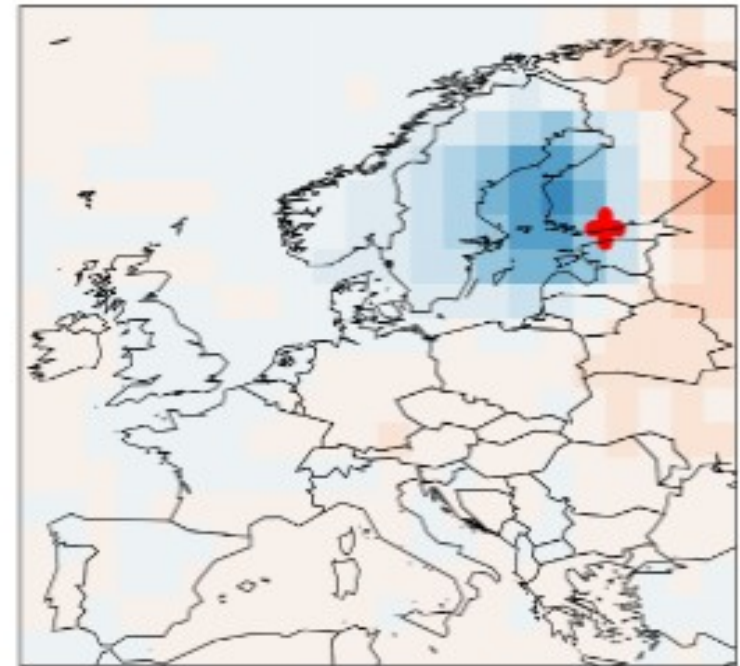
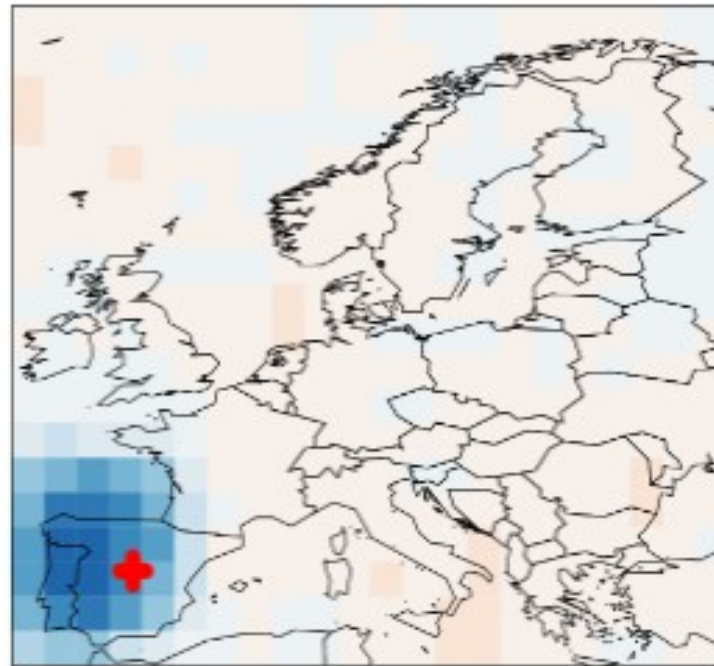
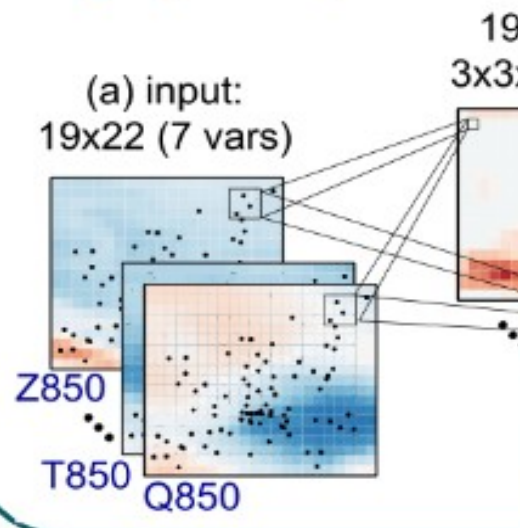




## Pros and Cons

### Transfer Functions

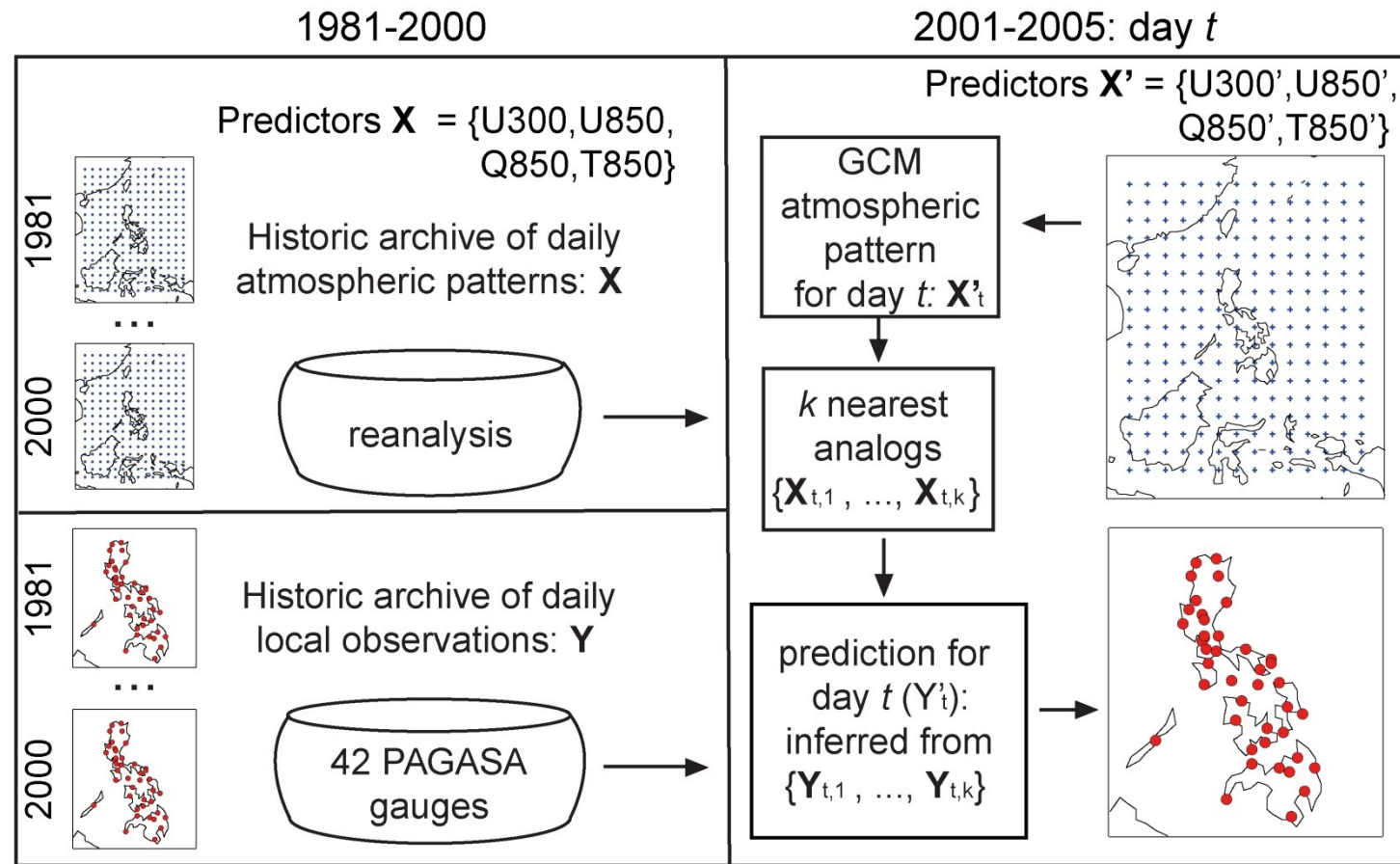
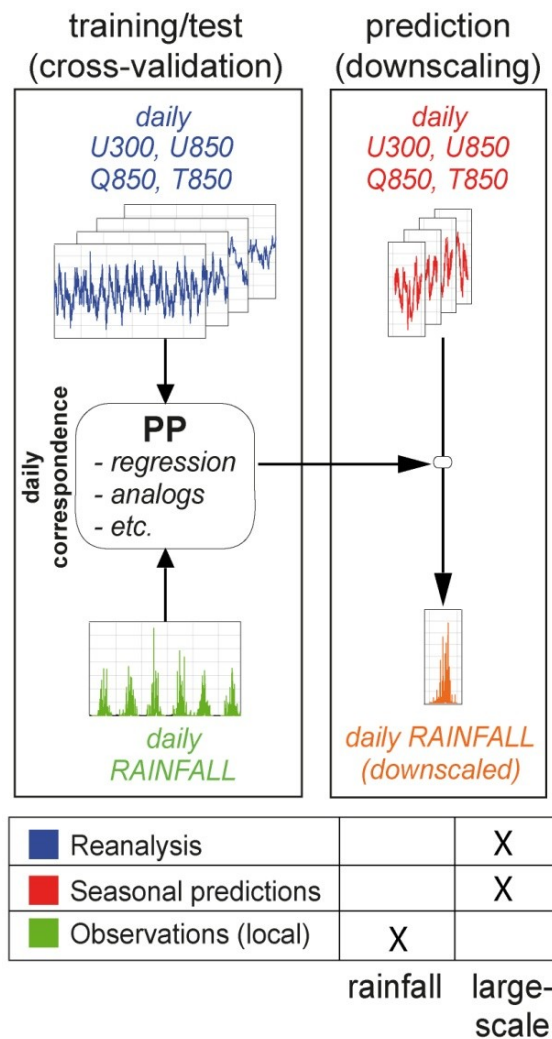
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# Statistical Downscaling

## Analogues Weather Typing

Similar atmospheric patterns lead to similar meteorological conditions (Lorenz, 1969). Based on the K-nearest neighbor algorithm.



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Similar atmospheric patterns lead to similar meteorological conditions (Lorenz, 1969). Based on the K-nearest neighbor algorithm.

- **Deterministic Adaptation:** Consider the sub-daily data observed for the analogue day.
- **Stochastic Adaptation:** Randomly chosen a day from the k-nearest and consider the sub-daily data observed for this day.
- **Adaptation:** Weather generator based on k-nearest neighbors.



## **Transfer Functions**

- **Transitions between the last hour of the previous day and the first one of the target day could not be preserved.**
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## **Analogues Weather Typing**

- **The optimum number of nearest neighbors should be chosen.**
- **A purely analogue method can not obtain non-observed values or sub-daily patterns.**
- **Physical and spatial coherence between variables and location is preserved if the predictors and the analogue day are the same.**

## Weather Generators

Stochastic models able to generate artificial time series with similar statistical properties than the observed time series.

**Weather Generators have been commonly used to generate artificial time series, mainly for precipitation based on:**

- **A 1-lag Markov Model to simulate the occurrence:**

$$p_{01}(k) = P[X_t(k) = 1 | X_{t-1}(k) = 0]$$
$$p_{11}(k) = P[X_t(k) = 1 | X_{t-1}(k) = 1].$$

- **A theoretical statistical distribution for the precipitation amount:**

$$f(x) = \frac{(x/\beta)^{\alpha-1} e^{-x/\beta}}{\beta\Gamma(\alpha)}; \quad x, \alpha, \beta > 0.$$

- **All the parameters are adjusted using observations.**

[http://www.ipcc-data.org/guidelines/pages/weather\\_generators.html](http://www.ipcc-data.org/guidelines/pages/weather_generators.html)

# Statistical Downscaling

## Weather Generators

Stochastic models able to generate artificial time series with similar statistical properties than the observed time series.

The most commonly approach is based on the work of Richardson (1981) and they are referred to as Richardson-type weather generators:

- A multi-variate weather generator: precipitation, temperatures and solar radiation.
- The seasonal cycle is explicitly considered/adjusted.
- Lag-0 and lag-1 cross-correlations between variables are preserved by means of a first-order linear autoregressive model for the residuals.
- Temperature and solar radiation are conditioned to the precipitation occurrence.

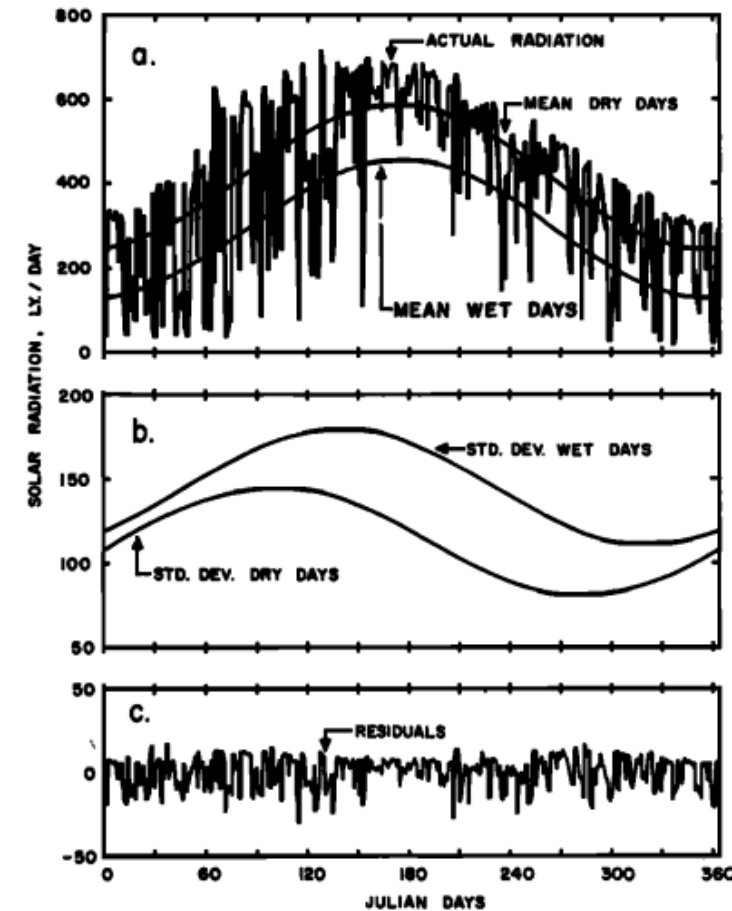


Fig. 1. Technique for reducing a daily solar radiation series to a series of residual elements, conditioned on the wet or dry status of the day.

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- **Temperature and solar radiation are conditioned to the precipitation occurrence. ← Some authors don't consider this dependence.**
- **Has been generalized to a multi-site approach and/or other variables (Peleg et al. 2017, Legasa et al. 2020).**



## ***Pros and Cons***

### **Transfer Functions**

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### **Weather Generators**

- **Parametric approaches should define the theoretical distributions of the different variables considered. In addition, the relations between variables is also established by the auto-regressive model considered.**
- **The statistical parameters adjusted by the weather generator are predefined by the user leading to very local and overfitted models.**
- **The transitions between days could be adjusted.**

## Analogue-based downscaling

Most of the temporal statistical downscaling methods are based on function/algorithm/weather generator applied to a previous set of  $k$  analogue days.

**In summary, this is the basic algorithm:**

- **K-nearest neighbors are obtained with daily data:**  $[Y_1^d, \dots, Y_k^d]$
- **For each neighbor, the distance to the target day ( $d$ ) is estimated:**

$$D_1^d = \sqrt{\sum (Y_1^d - d)^2}$$

- **This distance is used to obtain the hourly values of the target day ( $d$ ):**

$$[d_{01}, \dots, d_{24}]$$

- **The hourly values are rescaled to preserve the daily value.**

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- **Some authors consider a random resampling.**
- **Genetic algorithms (reproduction, crossover and mutation).**
- **...**

Rajagopalan, B., and Lall, U. (1999), A k-nearest-neighbor simulator for daily precipitation and other weather variables, *Water Resour. Res.*, 35( 10), 3089– 3101, doi:10.1029/1999WR900028.

Buishand, T. A., and Brandsma, T. (2001), Multisite simulation of daily precipitation and temperature in the Rhine Basin by nearest-neighbor resampling, *Water Resour. Res.*, 37( 11), 2761– 2776, doi:10.1029/2001WR000291.

Taesam Lee, Changsam Jeong, Nonparametric statistical temporal downscaling of daily precipitation to hourly precipitation and implications for climate change scenarios, *Journal of Hydrology*, 510, 2014, Pages 182-196, <https://doi.org/10.1016/j.jhydrol.2013.12.027>.



## **Analogue-based downscaling**

- **Are the most commonly used methods.**
- **Physical and spatial coherence between variables and locations could be preserved, or partially preserved, by means of the analogue method.**
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# **Thank you !!!!**

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