## **Energy Fluctuations & Extremes**

ISIMIP winter workshop, January 11, 2021

## Outline

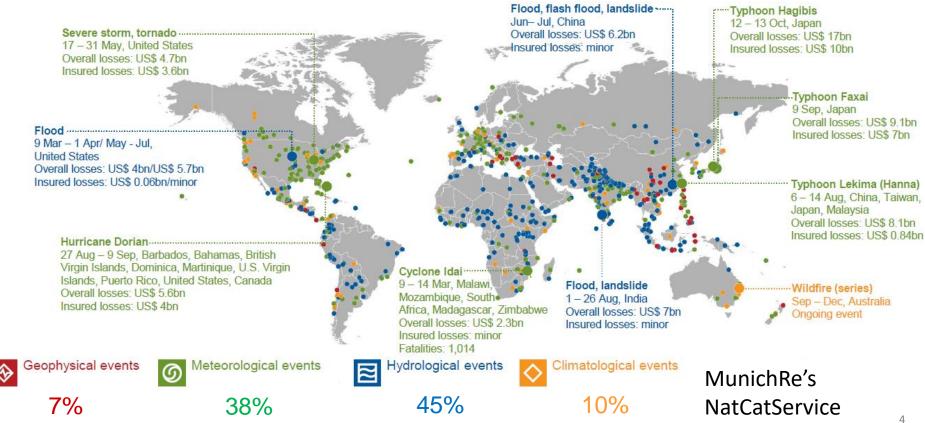
- Part 1 (~15mins)
  - → Short overview of the The Inter-Sectoral Impact Model Intercomparison Project (<u>www.ISIMIP.org</u>)
- Part 2 (~45mins)
  - $\rightarrow$  Introduction of the Energy Fluctuations & Extremes track
  - $\rightarrow$  Presentations of the different modeling approaches
- Part 3 (~30mins)
  - → Discussion on input data needs and first steps towards an ISIMIP3 protocol for this track

# How does climate change affect natural and human systems already today?

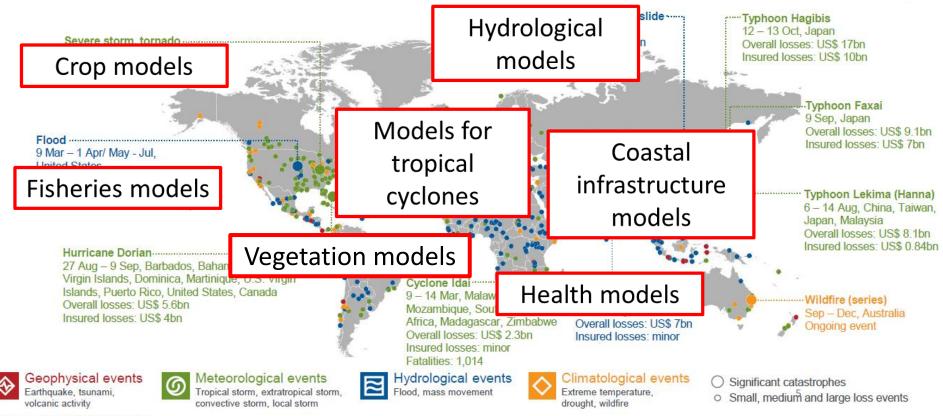
## How will it do so in the future?



#### Economic losses induced by weather extremes in 2019



## Future projections need a range of different impact models

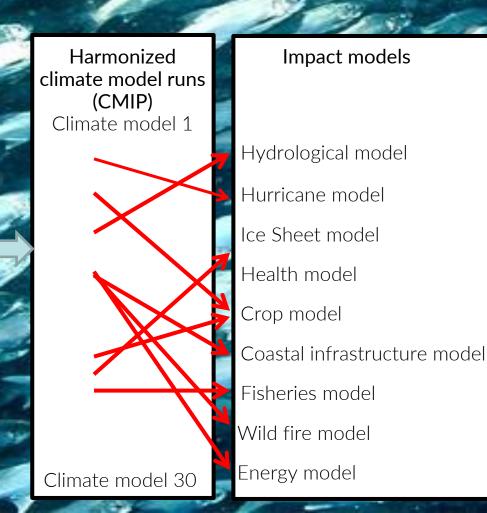


Source: Munich Re, NatCatSERVICE, 2019

### Pre-ISIMIP era

Common future Emission pathways (RCPs)

> RCP2.6 RCP4.5 RCP6.0 RCP8.5





## Aim of ISIMIP project.

Common future Emission pathways (RCPs)

> RCP2.6 RCP4.5 RCP6.0 RCP8.5

Harmonized climate model runs (CMIP) Climate model 1 Climate model 30

Impact models

Hydrological model

Hurricane model

Ice Sheet model

Health model

Crop model

Coastal infrastructure model

**Fisheries model** 

Wild fire model

Energy model

## Climate Impact Science

The World Climate Research Programme's Coupled Model Intercomparison Project

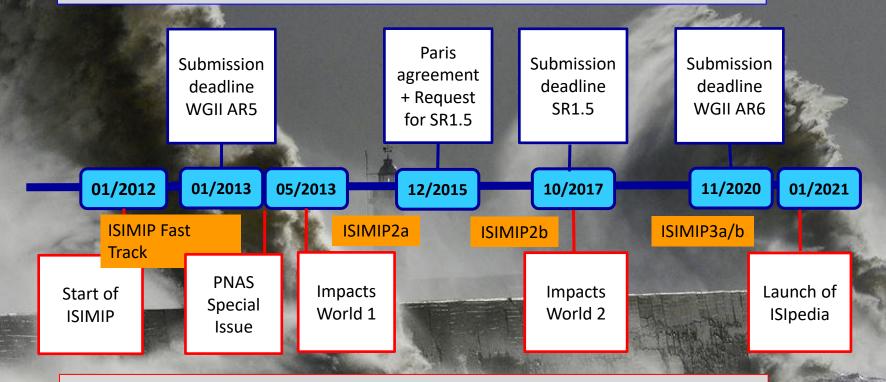
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S.C.



www.ISIMIP.org

## **External forcing: IPCC deadlines**



## **ISIMIP timeline**

## How ISIMIP works

Provided by ISIMIP coordination team

Climate data (daily, 0.5° x 0.5°) Historical observations + Projections CMIP 6 (bias corrected)

Socio-economic input (population, land-use, GDP, agricultural + water management)

Historical observations + Future Projections (SSP) Contributed by sectoral modelers

Impact Models (global + regional)

- Water
- Agriculture
- Coastal infrastructure
- Biomes
- Health
- Permafrost
- Energy
- Biodiversity
- Marine Ecosystems

Joint outcome

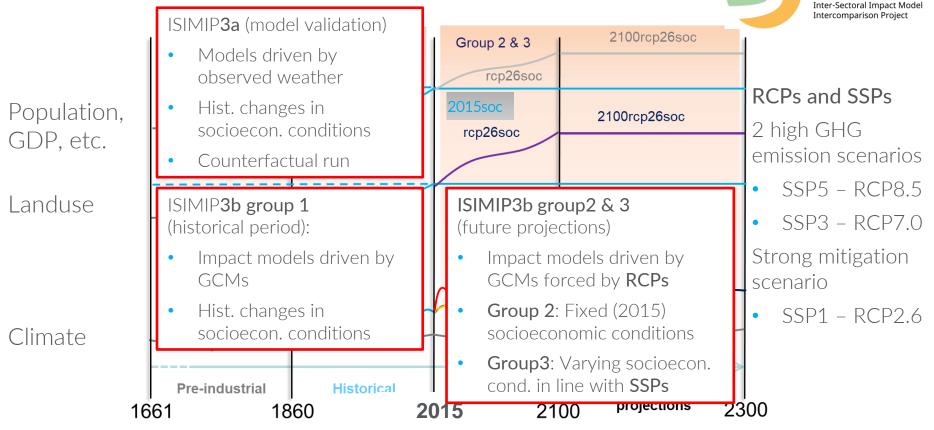
#### Main objectives

Cross sectorally consistent, temporally and spatially explicit impact analyses

٠

- Model validation
- Impact attribution
- Assessements of future climate risks

## ISIMIP – The modeling protocol



• Process based simulations permit separation of climate and socio-economic drivers

## Overview of input data (relevant for Energy Sector)

**Atmospheric variables** (reanalysis datasets 1901-2016 and CMIP6 (bias corrected) 1901-2016 & 2015-2100), daily time step, 0.5°:

→ Near-surface air temperature, surface down-welling radiation (longwave, shortwave), near-surface wind speed, precipitation, evapotranspiration, soil moisture, near surface air pressure

#### Biophysical variables:

- $\rightarrow$  From water models:
  - River runoff/discharge
  - Flood affected areas accounting for present day protection levels (18 arcsec)
- $\rightarrow$  From tropical cyclone models:
  - Storm tracks and wind fields

#### Socioeconomic data

 $\rightarrow$  Gridded population, GDP, land-use patterns, dam locations, ...

Plans to downscale to 1km x 1km and 3 hourly resolution

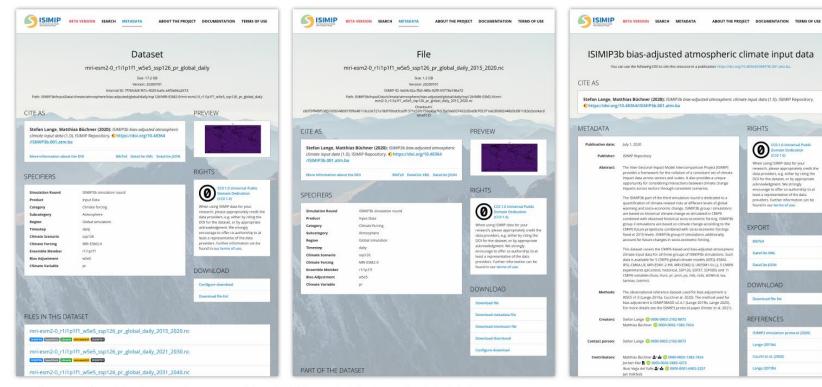
→ Session on Climate Forcing Data, today 4.15pm

## Archive for ISIMIP3 data

BETA	VERSION SEARCH METADATA ABOUT THE PROJECT DOCUMENTATION TERMS OF USE								
Search the ISIMIP	Search the ISIMIP Data Portal								
mri pr	Search <b>Q</b> Reset <b>X</b>								
Sidebar view:      Tree Facets	Show only the latest version Show specific versions with date constraints     Show archived files								
ISIMIP3a simulation round	Selection You selected 0 dataset of 0 B size. 10 datasets found.								
ISIMIP3b simulation round									
Input Data	Search constraints tree = ISIMIP3b/InputData/climate × query = mri pr × Download file list for this search								
Climate forcing									
Atmosphere	ISIMIP3b         InputDate         mri-esm2-0         10.48364/ISIMIP3b.001.atm.ba         ToU         CC0 1.0         20200701           mri-esm2-0_r1i1p1f1_w5e5_ssp126_pr_global_daily								
Atmospheric composition	Select dataset Show attributes > Show files > Configure download Download file list Download all files								
Lightning									
Ocean	ISIMIP3b         InputData         mri-esm2-0         10.48364/ISIMIP3b.001.atm.ba         ToU         CC0 1.0         20200701           mri-esm2-0_r1i1p1f1_w5e5_ssp126_prsn_global_daily								
Geographic data and inform									
Socioeconomic forcing									
	ISIMIP3b [InputData] mri-esm2-0_r1i1p1f1_w5e5_ssp370_pr_global_daily								

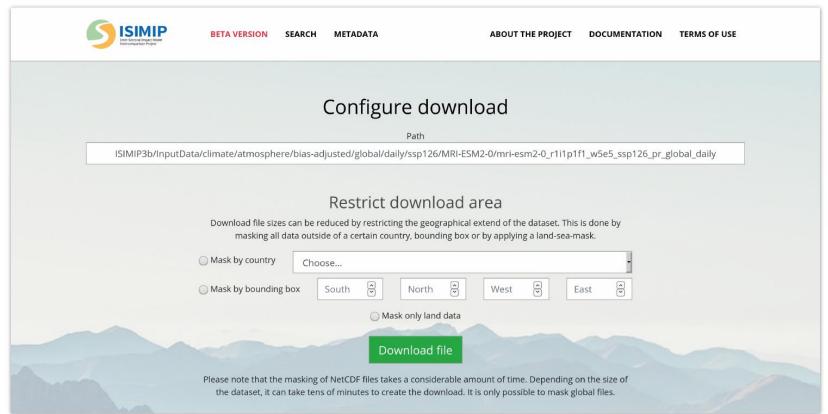
#### www.data.isimip.org

#### Datasets, Files, DOIs



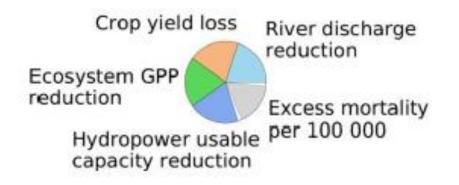
e.g. https://data.isimip.org/datasets/7f7b5dc8-f67c-4029-ba0c-e4f3e66a2673/

## **Tailored downloads**



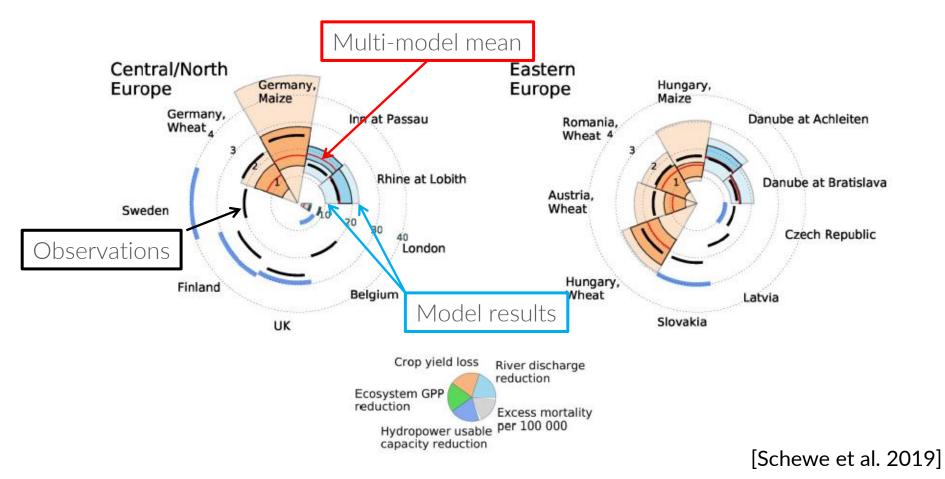
- Bulk downloads via wget
- ISIMIP-API

#### Example - Multi-sector impact analysis of 2003 European heatwave



[Schewe et al. 2019]

## Example - Multi-sector impact analysis of 2003 European heatwave



## What are the benefits in participating?

- ... aside from being a part of a thriving community of impact modelers at the forefront of science ...
- Influence on focus topics / protocol / ISIMIP input data (e.g., downscaled and harmonized data)
- Access to all ISIMIP output data embargo period for exclusive use within ISIMIP community
- Lots of exciting (cross-sectoral) studies (papers written in embargo period should offer coauthorship to all modeling teams whose data are used in the paper)

 $\rightarrow$  Paper writing workshops

• Synergies with existing modeling efforts (e.g., sector specific MIPs)

Requirements:

- Output data submitted to ISIMIP have to adhere to certain standards/formats specified in the protocol
- Publication of data on ESGF for public use

## **Energy Fluctuations & Extremes**



Potsdam Institute for Climate Impact Research

## Main research questions

- How will changes in weather variability and extremes
- ... impact on biophysical potentials, potential **supply**, and usable capacity?
  - E.g., how does usable capacities of thermal and hydro power plants change due to water shortages and high water temperatures under global warming?
- .... change demand
  - How does frequency of high cooling/heating episodes changes under global warming?
  - Can this induce short-term supply-demand mismatches (in the present day power system infrastructure)?
- How will **damages** of extreme weather events **to the energy infrastructure** affect power supply?
  - Cascading failures induced by tropical cyclones

## Long-run Climate Change Induced Impacts on Energy Systems

	Gradual climate change	Fluctuations & Extremes	Damages induced by weather extremes
Energy supply	Renewable potential (wind, solar, biomass, hydro)	Renewable reliability (wind, solar, biomass, hydro)	<ul> <li>Tropical cyclones breaching power poles</li> <li>Fluvial floods interrupting power plant operation</li> </ul>
	IAMs, Energy models	System regulators, Electricity models	Power grid models, Energy system models
Energy demand	<ul> <li>Long term changes in cooling and heating demand</li> </ul>	<ul> <li>Changes in frequency of episodes with high cooling/heating demands</li> </ul>	
	IAMs, Energy models		
Validation		<ul> <li>Historical episodes with low renewable supply and high energy demand</li> </ul>	Historical power outages and reconstruction periods

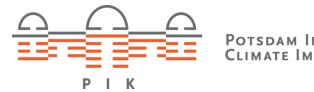
## Impacts of Changes in Fluctuations and Extremes on Energy Systems

	Gradual climate change		Fluctuations & Extremes	Damages induced by weather extremes
Energy supply	<ul> <li>Renewable potential (wind, solar, biomass, hydro)</li> <li>IAMs, Energy models</li> </ul>		<ul> <li>Renewable reliability (wind, solar, biomass, hydro)</li> <li>Electricity models, Energy system models</li> </ul>	<ul> <li>Tropical cyclones breaching power poles</li> <li>Fluvial floods interrupting power plant operation</li> <li>Power grid models, Energy system models</li> </ul>
Energy demand	<ul> <li>Long term changes in cooling and heating demand</li> <li>IAMs, Energy models</li> </ul>		<ul> <li>Changes in frequency of episodes with high cooling/heating demands</li> </ul>	
Validation		<ul> <li>Historical episodes with low renewable supply and high energy demand</li> </ul>	<ul> <li>Historical power outages and reconstruction periods</li> </ul>	

## Short introduction of modeling approaches

- 1. Global hydropower and thermoelectric power vulnerability to climate and water resources changes and variability, **Michelle van Vliet**, Univ. of Utrecht, Netherlands
- 2. Water Risk for the Bulk Power System: Asset to Grid Impacts, Ariel Miara, National Renewable Energy Laboratory, USA
- 3. Meteorological conditions leading to extreme low variable renewable energy production and extreme high energy shortfall, **Karin van der Wiel**, Royal Netherlands Meteorological Institute
- 4. Wind and solar power modeling, Robert Vautard, Institut Pierre-Simon Laplace, France
- 5. Methods to explore Climate impacts on zero carbon energy system mitigation pathways in TIMES-GEO, **James Glynn**, MaREI-UCC, Ireland
- 6. Clim2power impacts of climate variability for a carbon-neutral EU power sector, **Sofia Simões**, National Laboratory of Energy and Geology, Portugal
- 7. Investigating the Risk of Hurricane-Induced Cascading Failures in Power Systems of the U.S. East Coast, Julian Stürmer, Potsdam Institute of Climate Impact Research, Germany

## Protocol



Potsdam Institute for Climate Impact Research

## The ISIMIP3 protocol

ISIMIP3a: Model validation for extended historical period (varSoc)

- Climatic forcing according to observed weather
- Observed changes in socioeconomic drivers

Requires:

- Database capturing historical changes in **energy infrastructure** 
  - e.g., Global Power Plant Database, WRI
- Historical data on power grids
- Datasets for model validation
  - Historical data on energy supply and demand
  - Historical impacts of extremes on power supply
- Focus regions or global?
  - For which regions beyond the US are good data available?

Start community data-collection effort in ISIMIP?

## The ISIMIP3 protocol

ISIMIP3a: Model validation for extended historical period (varSoc)

- Climatic forcing according to observed weather
- Observed changes in socioeconomic drivers:

**ISIMIP3b**: Climatic forcing provided by (bias corrected) GCMs

- **Group1**: historical period, varSoc
- **Group2**: future period, 2015soc
  - Climatic forcing changes according to RCP scenarios
- **Group3**: future period, varSoc
  - Socioeconomic conditions (e.g., energy infrastructure) varies according to SSPs

## Overview of input data (relevant for Energy Sector)

**Atmospheric variables** (reanalysis datasets 1901-2016 and CMIP6 (bias corrected) 1901-2016 & 2015-2100), daily time step, 0.5°:

→ Near-surface air temperature, surface down-welling radiation (longwave, shortwave), near-surface wind speed, precipitation, evapotranspiration, soil moisture, near surface air pressure

Biophysical variables:

- $\rightarrow$  From water models:
  - River runoff/discharge
  - Flood affected areas accounting for present day protection levels (18 arcsec)
- $\rightarrow$  From tropical cyclone models:
  - Storm tracks and wind fields

Plans to downscale to 1km x 1km and 3 hourly resolution

Further needs on atmospheric data and biophysical impact data?

### Next steps

- Let us know whether you would like to participate
- <u>Link to ISIMIP3 protocol paper</u> (in preparation)
- Review paper?
- Follow-up meetings to discuss input data needs and protocol development

## Impacts of Changes in Fluctuations and Extremes

	Gradual climate change		Fluctuations & Extremes	Damages induced by weather extremes
Energy supply	<ul> <li>Renewable potential (wind, solar, biomass, hydro)</li> <li>IAMs, Energy models</li> </ul>		<ul> <li>Renewable reliability (wind, solar, biomass, hydro)</li> <li>System regulators, Electricity models</li> </ul>	<ul> <li>Tropical cyclones breaching power poles</li> <li>Fluvial floods interrupting power plant operation         Power grid models, Energy system models     </li> </ul>
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# Global hydropower and thermoelectric power vulnerability to climate and water resources changes and variability

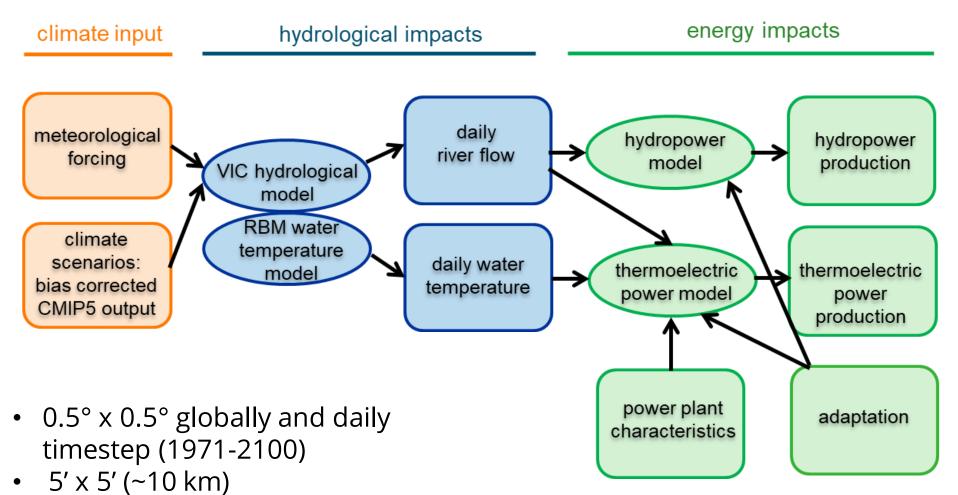


#### Dr. Michelle van Vliet

Assistant Professor, Department of Physical Geography, Utrecht University, The Netherlands ISIMIP workshop session energy fluctuations and extremes, 11 January 2020

## Global model framework

To study hydropower and thermoelectric power plant vulnerability to climate change and variability

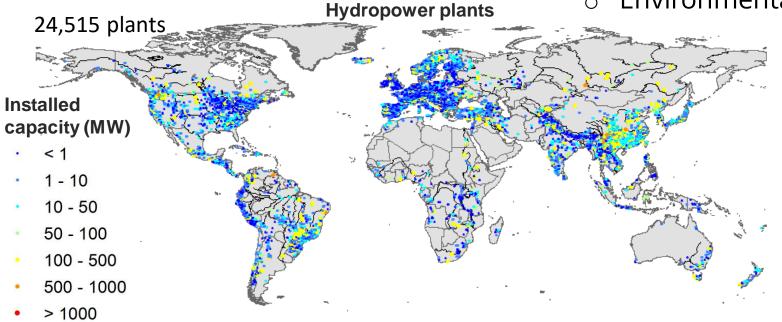


## Input data

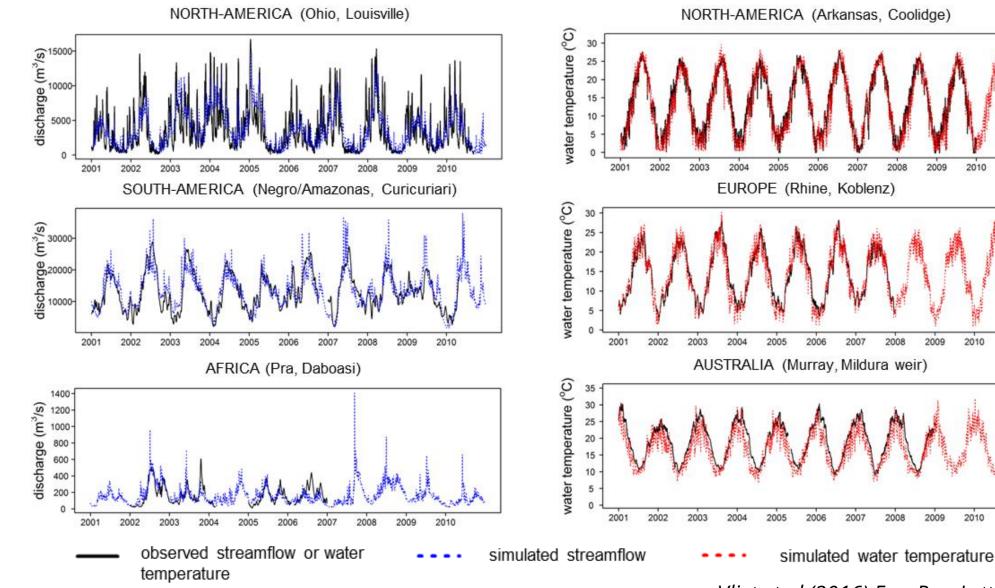
- World Electric Power Plant Database (WEPPD)
- Hydropower:
  - Simulated discharge
  - o Hydraulic head
  - o Efficiency
  - Installed capacity

## • Thermoelectric power:

- Daily discharge and water temperature
- o Efficiency
- Installed capacity
- Cooling system type
- Environmental limitations

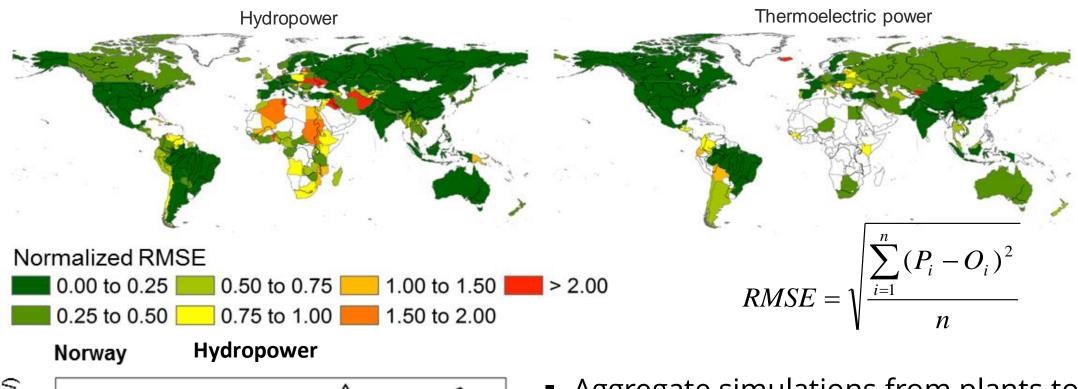


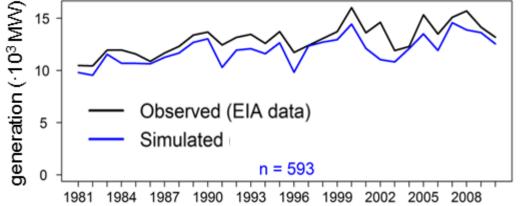
## Model validation discharge and water temperature



van Vliet et al (2016) Env. Res. Lett.

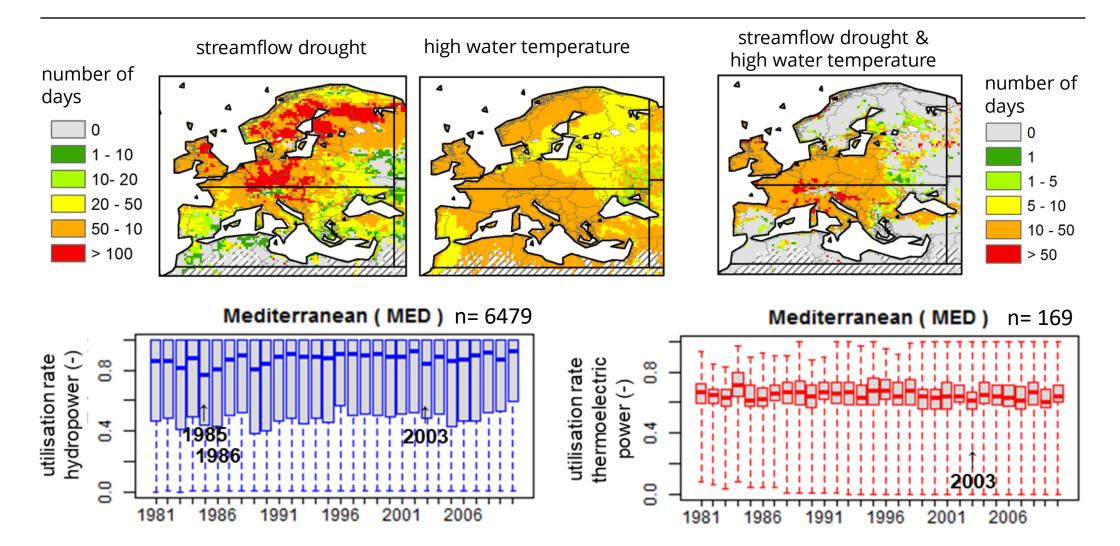
## Model validation





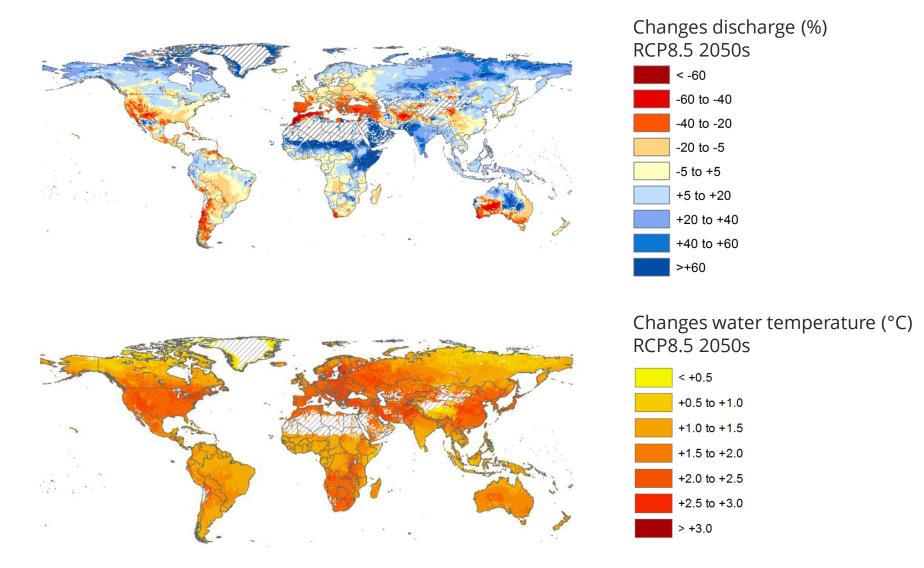
 Aggregate simulations from plants to country level (annual timestep) to compare with reported values of EIA

## Impacts of European 2003 drought



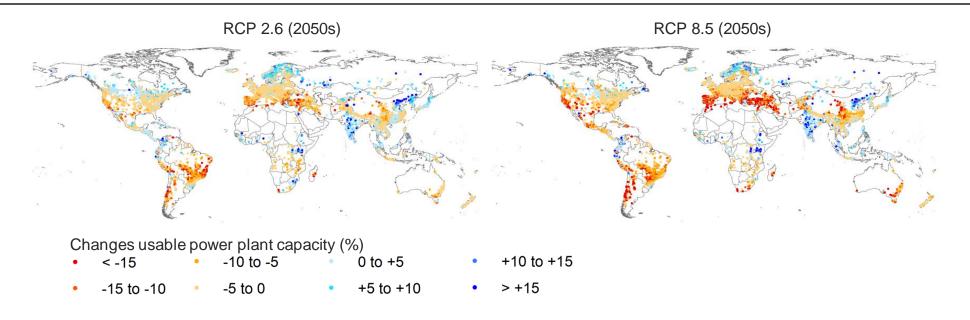
**2003 European drought:** reductions of 6.6% in hydropower and 4.7% in thermoelectric power compared to long-term average for 1981-2010 *van Vliet et al (2016) Env. Res. Lett.* 

## Climate change impacts on discharge and temperature

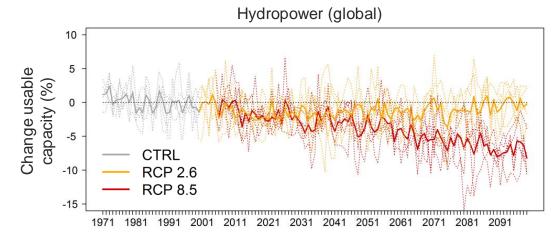


van Vliet et al (2016) Global Environmental Change

### Climate change impacts on hydropower



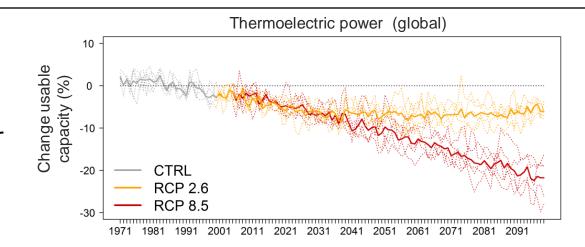
- Declines projected for 61 74% of the hydropower plants
- Global reductions of **1.2 3.6%** for RCP2.6 - RCP8.5 (2050s)



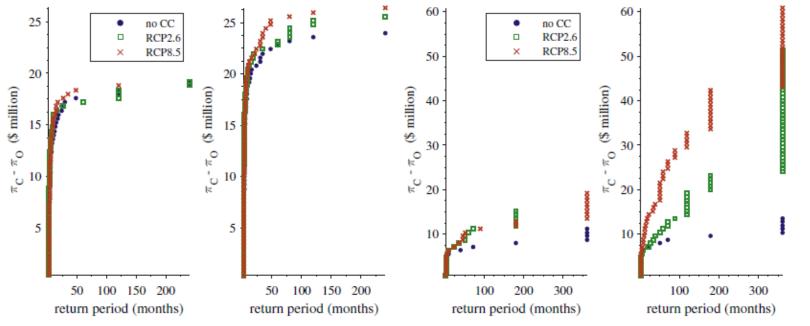
van Vliet et al (2016), Nature Climate Change

### Climate change impacts on thermoelectric power

- Declines projected for 81 86% of the thermoelectric plants
- Global reductions of **7 12%** for RCP2.6 - RCP8.5 (2050s)



Lost power plant profits due to decreased thermoelectric power plant usable capacities



Bogmans et al (2018) Energy Economics

## Thank you very much!



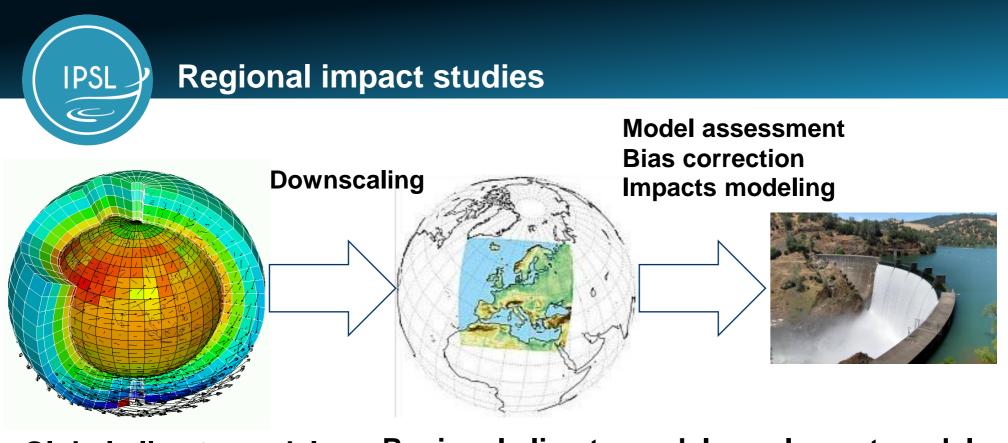
Contact: Dr. Michelle van Vliet <u>m.t.h.vanvliet@uu.nl</u>





### Wind & solar modeling for climate impacts

Robert Vautard Institut Pierre-Simon Laplace



Global climate model (100-300 km) Regional climate model (10-50 km)

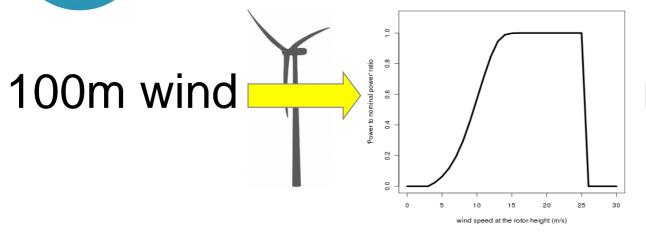
Impact model

→ MED-CORDEX: new coupled simulations, processes
 → EURO-CORDEX : now~65 GCM-RCM projections (12 km)
 → To come: Convection permitting simulations



### Wind / solar power load factor

Normalized power curve (VESTAS V90-3MW)





**In models**: requires hourly 100 m (or 80 or 150) winds

- → Usually 10m winds available (very different diurnal profile)
- → Usually daily data available only
- → Now consider several technologies

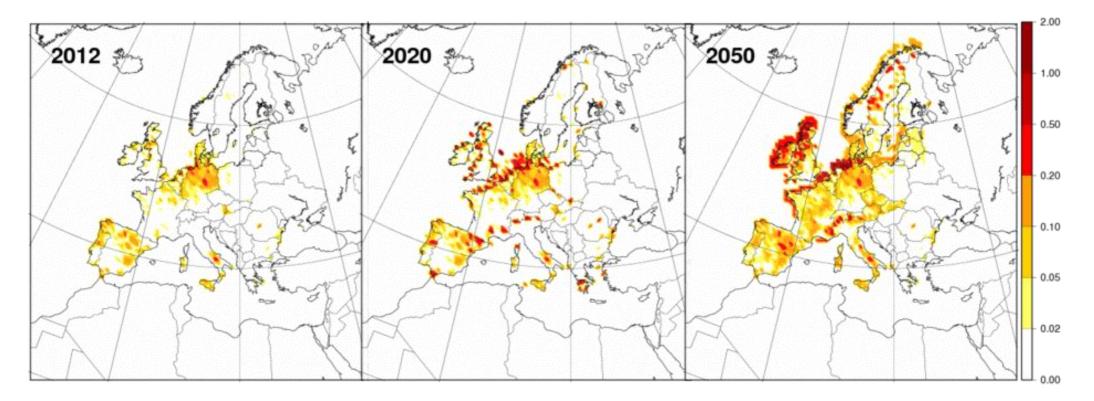
**Solar power (PV)**: requires radiation, cloudiness, wind, temperature

- → Usually oversimplified formulae using global radiation
- → Recent progresses to include:
  - → Direct/diffuse radiation decomposition
  - → Separate rooftop, central with/without dual trackers

**IPSL** 



### Tobin et al., 2018



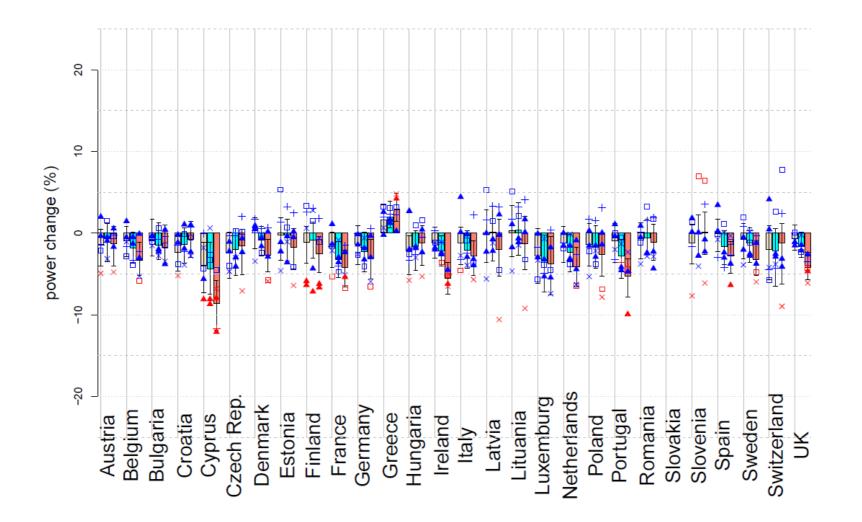
Installed wind power according to 60% or 80% REs in 2050 (here 80%), 450 GWatts





# Wind Power Changes for a 1.5°C, 2°C and 3°C global warming level

5 Euro-Cordex models used (Tobin et al., 2018, ERL)





- IMPACT2C (H2020) : estimating impacts for energy systems for 1.5°C and 2°C warming
- C3S Energy: CLIM4ENERGY demonstrator, then operational services
- EUCP (H2020) : case study on impacts for wind droughts estimation for producers or countries (see below)
- Several industry-led climate services projects (scenarios 2050, risk analysis)



# WIND POWER DROUGHTS: Change in intensity of 20-year return events of low-seasonal events

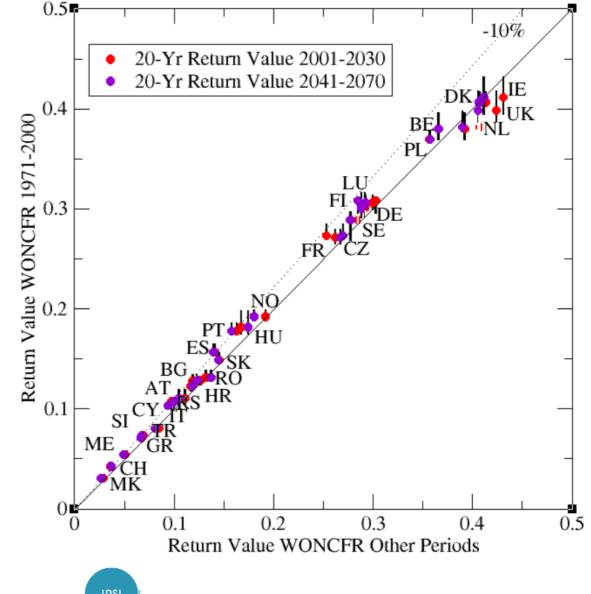
Using the C3S Energy projections (bias corrected) of the wind power load factor

Averaging over countries the load factor and over the winter season

Pooling models

Calculating extreme statistics (nonparametric method) over 2 time periods

H2020 EUCP Project





### **Types of extremes for Res / Transmission network:**

- Wind « droughts »
- Wind storms
- Low radiation extremes
- Heat waves (risks for power lines)
- Unbalanced loads

### **Attribution of extremes/events**:

- How does the current extreme relate to climate change
- Can be applied to Res but also most types relating to energy sector (eg heat wave, cold spell, hydro drought, storms, wind/solar power bad seasons, ...)





# Thanks for your attention!

Robert Vautard Institut Pierre-Simon Laplace





Clim2power - impacts of climate variability for a carbon-neutral EU power sector



Cross-sectoral ISIMIP and PROCLIAS online workshop 2021 ISIMIP Sector meeting: Energy (Fluctuations and extremes)

LNEG Sofia G. Simões<sup>1</sup>, Edi Assoumou<sup>2</sup>, Gildas Siggini<sup>2</sup>, V. Sessa<sup>2</sup>, Y-M., St. Drenan<sup>3</sup>, S. Carvalho<sup>4</sup>, P. Fortes<sup>5</sup>, et al.

<sup>1</sup>LNEG, <sup>2</sup>ARMINES CMA - Sophia Antipolis, <sup>3</sup>ARMINES OIE, <sup>4</sup>FCUL Lisbon University, <sup>5</sup>CENSE–FCT NOVA University Lisbon





### Key information

**modeling approach** Energy (power) systems optimization model: *eTIMES-EU* Unit commitment model -*DispaSET* 

## spatial and temporal scales of the model

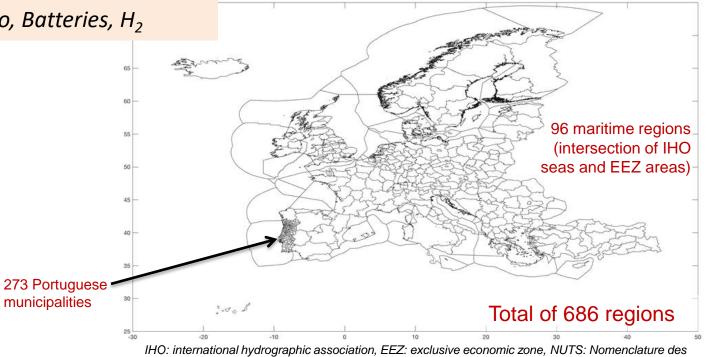
National level (but NUT2 capacity factors) *eTIMES-EU:* 3hr, week and weekend days for each season, 2016-2060 *DispaSET:* hourly, 2020

**focus regions** each EU country + UK, NO, CH, IS

#### covered technologies

whole power sector Solar PV Onshore and offshore wind Hydropower Gas, coal, nuclear, geothermal, bioenergy (...) Pumped hydro, Batteries, H<sub>2</sub>

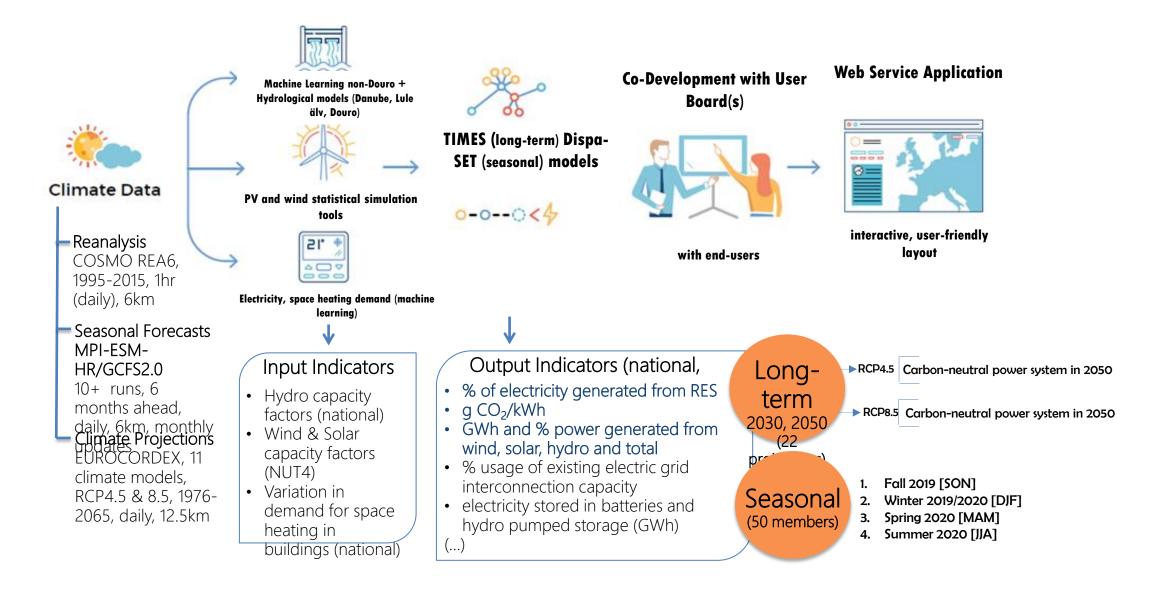
#### Capacity factors for solar and wind for 263 NUTS2 regions for Europe



unités territoriales statistiques



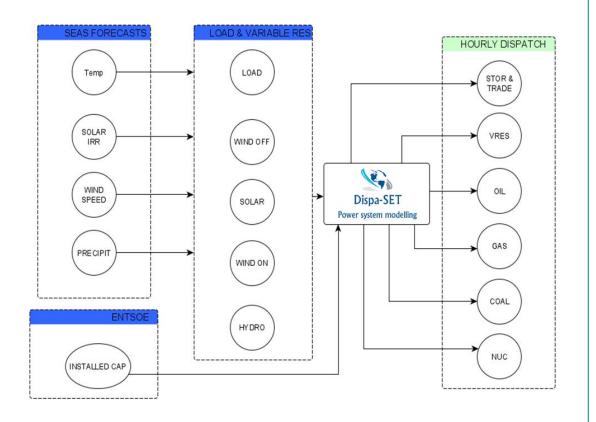
# Clim2Power Pipeline – from climate data to energy/power indicators



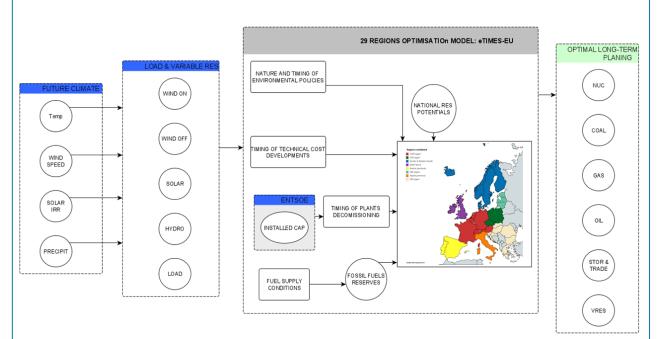


### Models for interconnected power system in Europe (each country is disaggregated)

## Seasonal Forecasts: Dispa-SET unit commitment model (hourly balancing)



Long-term Projections: eTIMES-EU cost minimisation model (3hr, week and weekend days for each season)



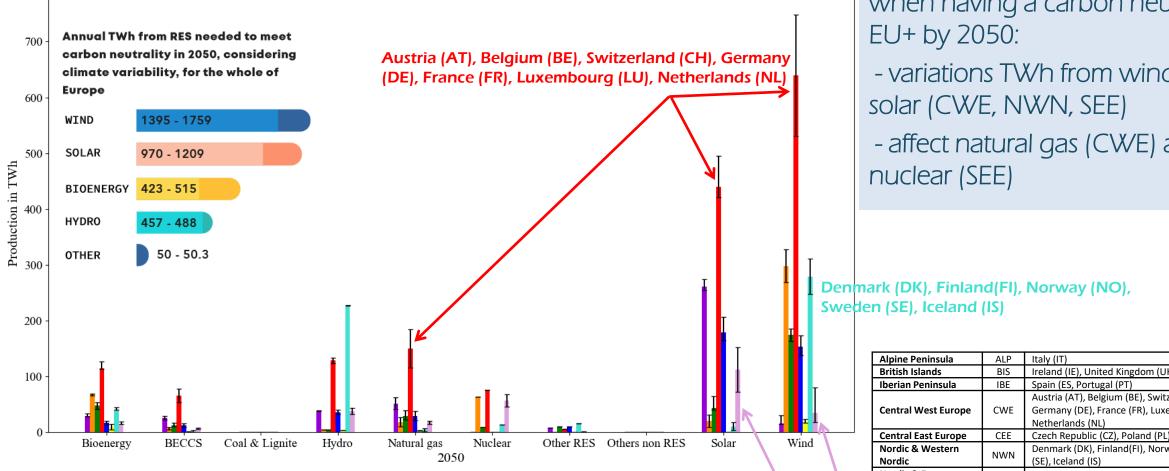
Run for 22 climate projections, 2016-2050, carbon neutral by 2050

Run for all ensemble members in each forecast



### Long-term $\rightarrow$ Generated power in 2050 (TW/h)





Bulgaria (BG), Greece (GR), Croatia (HR), Hungary (HU), Romania (RO), Slovenia (SI), Slovakia (SK)

By considering climate projections when having a carbon neutral

- variations TWh from wind and

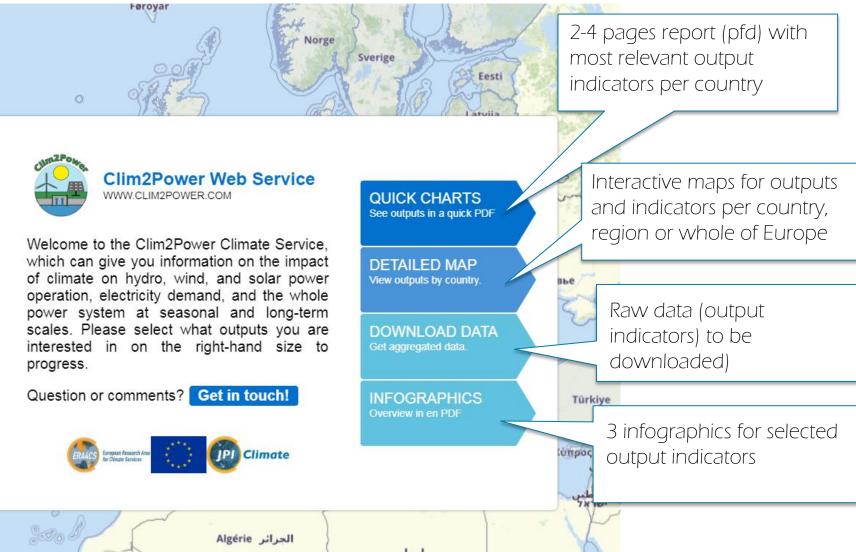
- affect natural gas (CWE) and

Alpine Peninsula	ALP	Italy (IT)
British Islands	BIS	Ireland (IE), United Kingdom (UK)
Iberian Peninsula	IBE	Spain (ES, Portugal (PT)
		Austria (AT), Belgium (BE), Switzerland (CH),
Central West Europe	CWE	Germany (DE), France (FR), Luxembourg (LU),
		Netherlands (NL)
Central East Europe	CEE	Czech Republic (CZ), Poland (PL)
Nordic & Western	NWN	Denmark (DK), Finland(FI), Norway (NO), Sweden
Nordic		(SE), Iceland (IS)
Nordic & Eastern	NEE	Estonia (EE), Lithuania (LT), Latvia (LV)
Nordic		
South Eastern Europe	SEE	Bulgaria (BG), Greece (GR), Croatia (HR), Hungary
		(HU), Romania (RO), Slovenia (SI), Slovakia (SK)



### Clim2power webservice

### http://viewer.webservice-energy.org/clim2power/





### Thanks everyone!





### More on CLIM2POWER:

https://clim2power.com/ sofia.simoes@lneg.pt

Project CLIM2POWER is part of ERA4CS, an ERA-NET initiated by JPI Climate, and funded by FORMAS (SE), DLR (DE), BMWFW (AT), FCT (PT), EPA (IE), ANR (FR) with co-funding by the European Union (Grant 690462).



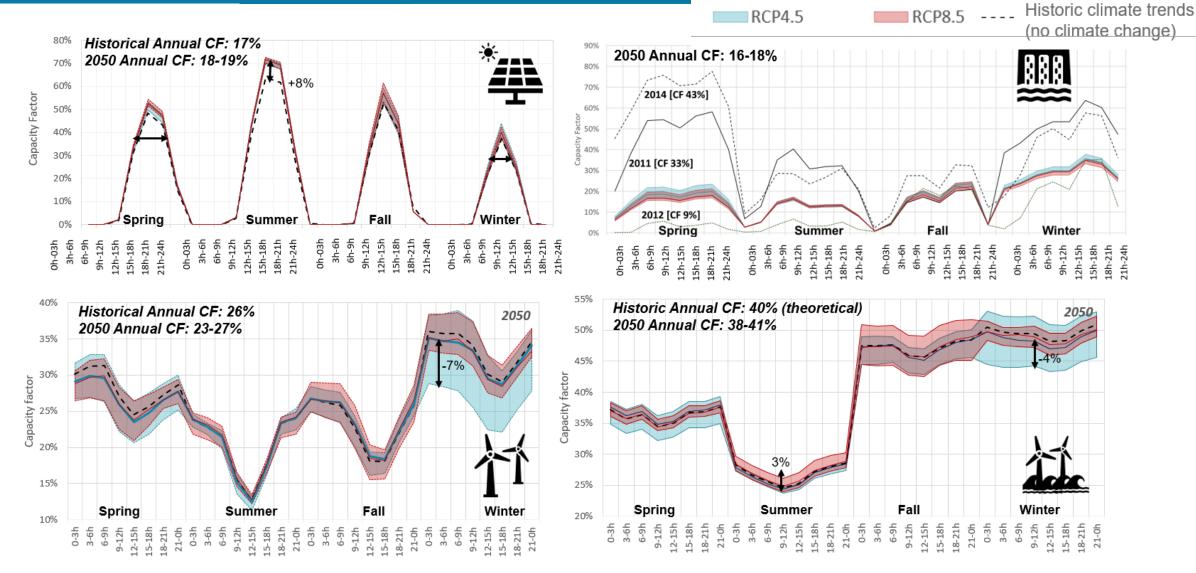
European Research Area for Climate Services







### How capacity factors could look like in 2050





#### Investigating the Risk of Hurricane-Induced Cascading Failures in Power Systems of the U.S. East Coast

Julian Stürmer

Julian.Stuermer@pik-potsdam.de

11.01.2021





#### **Motivation**

Collaboration:

#### Mehrnaz Anvari<sup>1</sup>, Anton Plietzsch<sup>1</sup>, Frank Hellmann<sup>1</sup>, Christian Otto<sup>2</sup>, Thomas Vogt<sup>2</sup>

<sup>1</sup> Research Department 4: Complexity Science (PIK)

<sup>2</sup> Research Department 3: Transformation Pathways (PIK)



#### **Motivation**

Collaboration:

Mehrnaz Anvari<sup>1</sup>, Anton Plietzsch<sup>1</sup>, Frank Hellmann<sup>1</sup>, Christian Otto<sup>2</sup>, Thomas Vogt<sup>2</sup>

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#### Idea: Study the impact of hurricanes on power grids

 $\rightarrow$  Combine two research topics:

- 1. Storm impact modeling (focus on power grids)
- Power grid modeling (focus on cascading failures)



Hurricane Laura, Sulphur, LA (August 30, 2020) Image courtesy of Entergy Louisiana



First step: Choose a geographical region of interest (e.g. Texas)

Storm impact modeling

Power grid modeling

Input Data

Algorithms

Results



First step: Choose a geographical region of interest (e.g. Texas)

Storm impact modeling

Power grid modeling

Input Data

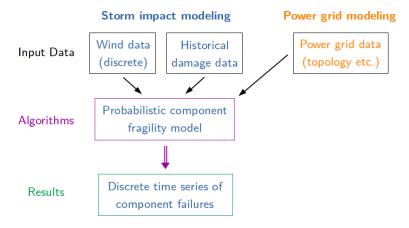
Wind data Historical (discrete) damage data Power grid data (topology etc.)

#### Algorithms

Results

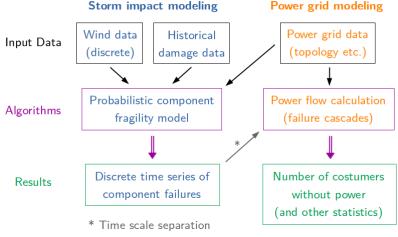






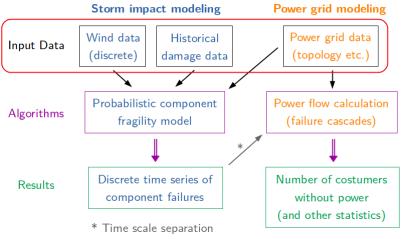






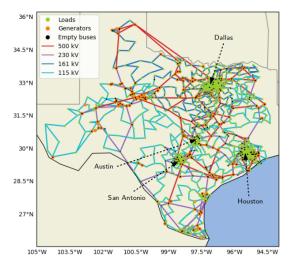


First step: Choose a geographical region of interest (e.g. Texas)





#### Synthetic Grid for Texas



Test case data with:

- 2000 buses
- 1125 load buses with ~ 70 MVA total load
- 432 generator buses ... in 1250 substations
- 861 transformers
- 2345 transmission lines
- 4 high voltage levels

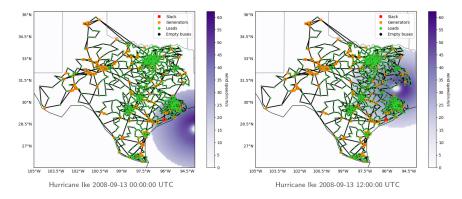
Grid data available at https://electricgrids.engr.tamu.edu/electric-grid-test-cases/



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#### Wind Data

- Wind fields calculated by Thomas Vogt using CLIMADA (Python) and historical storm tracks from IBTrACS
- For now:  $0.1^\circ \times 0.1^\circ$  spatial resolution and 1h time resolution



#### **Transmission Line Fragility**

Standard wind force design equation:

$$F_{\text{wind}}(\boldsymbol{\nu}, \boldsymbol{L}) = Q\boldsymbol{k}_{z}I_{\text{FW}}G_{\text{WRF}}(\boldsymbol{L})C_{\text{f}}A_{\text{C}}\boldsymbol{\nu}^{2}$$
(1)

Q - air density,  $k_z$  - terrain correction,  $I_{\rm FW}$  - importance factor, L - line length in m

Eq. (1) taken from ASCE Report 113, Substation Structure Design Guide (2007)

 $\rightarrow$  Damage probability for line *l*:

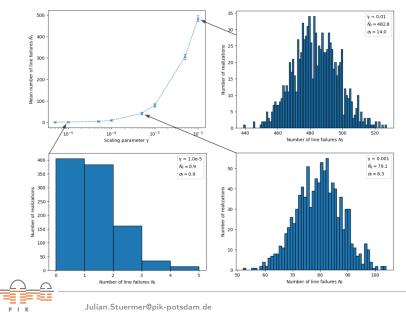
$$p_{\text{f,wind},l} = \min\left(\gamma \frac{F_{\text{wind},l}}{F_{\text{brk},l}}, 1.0\right), \qquad (2)$$

#### with scaling factor $\gamma$ and breaking load $F_{\text{brk},l}$

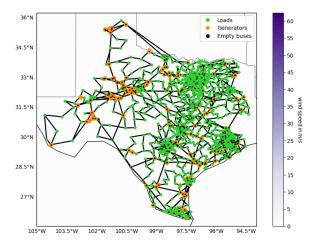
Eq. (2) taken from J. Winkler et al., Reliability Engineering and System Safety 95 (2010) 323-336



#### **Transmission Line Fragility Results**



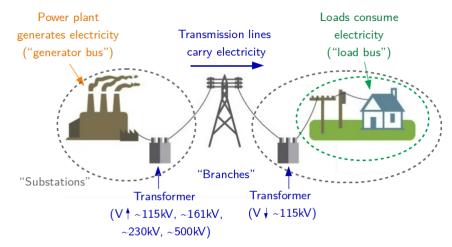
#### **Transmission Line Fragility Results**



Hurricane Ike (2008) passing over Texas ( $\gamma = 0.055$ )



#### **Power Grid Components**

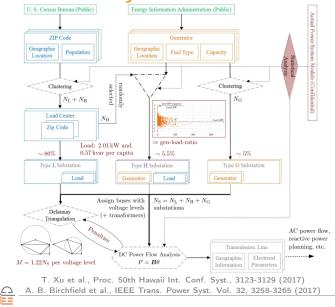


Source: Adapted from National Energy Education Development Project (public domain)



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#### **Transmission Grid Synthesis**



DIK

#### **AC Power Flow Equations**

Apparent power  $S_i = P_i + iQ_i = V_i I_i^*$ , voltage  $V_i = |V_i|e^{i\theta_i}$ , current  $I_i = \sum_{j=1}^N Y_{ij}V_j$ , admittance  $Y_{ij} = G_{ij} + iB_{ij}$ ,  $\Rightarrow P_i = \sum_{j=1}^N |V_i| |V_j| (G_{ij}\cos(\theta_i - \theta_j) + B_{ij}\sin(\theta_i - \theta_j))$ , (3)

$$\Rightarrow Q_i = \sum_{j=1}^N |V_i| |V_j| (G_{ij} \sin(\theta_i - \theta_j) - B_{ij} \cos(\theta_i - \theta_j)), \qquad (4)$$

Loads: PQ-buses with P, Q < 0 ( $|V|, \theta$  unknown) Generators: PV-buses with  $P, |V| = \text{const} (\theta \text{ unknown})$ Slack bus:  $|V|, \theta$  fixed and P compensates losses



https://github.com/lanl-ansi/PowerModels.jl



#### **Texas AC Power Flow**

